# Parametric Searching Algorithms with Adaptive Strategy for Three Dimensional Protein Structures Alignments 

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#### Abstract

Protein structure provides the opportunity to recognize homology that is undetectable by sequence comparison, and it represents a powerful means of discovering functions, yielding direct insight into the molecular mechanisms.

Currently, there are several techniques available in attempting to find the optimal alignment of shared structural motifs between two proteins. In this paper, we show the effectiveness of the proposed refinement methods [11] by a set of experiments, which have improved some previous results. We propose a better adaptive strategy to have better parameters, and we can get a better pairwise alignments of protein structures. We can apply this strategy to find more accurate and similar protein structure pairings.


Keywords: structural proteomics, alignments and comparisons, refinement, pretest algorithm

## 1 Introduction

Protein structures play a critical role in vital biological functions [7]. There are more and more protein structures determined by the advances in X-ray crystallography and NMR spectroscopy. Therefore, more and more people want to analyze and classify these protein structures in order to understand their relationships with protein functions [6].

Protein structures determine the protein function, we are now trying to chase down all possible relationship about human and all kinds of proteins. According to this reason, the comparisons

[^0]of protein structures come into existence, and some academics proposed some methods to compare protein structures such as DALI [9],VAST [15] and CE [21]. All of them can find the similarity score between two or more structures. Their structural alignments are a form of sequence alignment based on comparison of three-dimensional conformation. But they can only find the structural alignments with sequencing. Lin publishes another methods to compare proteins in terms of three dimensional protein structure alignments [14]. We can have better score by Lin's methods if we use the VAST alignment to be its initial alignment [11].

One of the primary goals of structural alignment programs is to quantitatively measure the level of structural similarity between all pairs of known protein structures. This data can provide several meaningful insights into the nature of protein structures and their functional mechanisms. The three dimensional structure of proteins is highly conserved during evolution [4]. Protein are constructed by one or more polypeptide chains that fold into complicated 3D structures.
Detection of proteins with a similar fold can suggest a common ancestor, and often a similar function [5]. Comparison of 3D structures makes it possible to establish distant relationships, even between protein families distinct in terms of sequence comparison alone. This is why structural alignment of proteins increases our understanding of more distant evolutionary relationships $[3,12]$. The link between structural classification and sequence families enables us to study functions of various folds, or whole proteins [14].
In this paper, first we introduce the process about why we develop the three parameters searching programs and what is the tools to compare protein structures in the literatures. Secondly, we explain about how to develop our methods and what our methods are. In the third part, we compare the results between our pro-
posed methods and the CE methods and then show the experimental results. In the third, we use a adaptive strategy to find the initial space without any suggestion and compare them with VAST and CE.

## 2 Previous Work

In this section, we introduce $r m s d$ which is the standard of measure for structural comparison, and then according to the rmsd we can find the key point, rotation matrix, which can rotate the 3D protein coordinates to the better place. Then, we can be easy to compare the rmsd between the rotated protein and the other protein. We can find the other critical analysis by Euler's rotation theorem [13], and we can use the three angles to stand for the rotation. But our methods are not the same as Euler's theorem. We become deformed the Euler's theorem and find another adaptable three angles for our programs. We point out the two important concepts. One is the rotation matrix, and another is the Minimum Bipartite Matching. Our previous programs integrate the two important components to compare protein structures. The algorithm is showed in figure 1.

### 2.1 Root mean squared deviation

The smallest root mean squared deviation (rmsd) is a least-squares fitting method for two sequences of points [10]. The idea is to align atom vectors of the two given (molecular) structures, and use the common least averaged squared errors as a measurement of differences between these two (paired) sequences. Formally, let $P=\left\langle p_{1}, \ldots, p_{n}\right\rangle$ and $Q=\left\langle q_{1}, \ldots, q_{n}\right\rangle$ be two sequences of points. We assume that $P$ is translated so that its centroid $\left(\frac{1}{n} \sum_{k=1}^{n} p_{k}\right)$ is at the origin. We also assume that $Q$ is translated in the same way. For each point or vector $x$, let $(x)_{i}(i=1,2,3)$ denote the $i$-th $(X, Y, Z)$ coordinate value of $x$, and $\|x\|$ denote the length of $x$. Let

$$
\begin{equation*}
\operatorname{RMSD}(P, Q, R, \mathbf{a})=\sqrt{\frac{1}{n} \sum_{k=1}^{n}\left\|R p_{k}+\mathbf{a}-q_{k}\right\|^{2}}, \tag{1}
\end{equation*}
$$

where $R$ is a rotation matrix and $\mathbf{a}$ is a translation vector. Then, the rmsd value $d(P, Q)$ between $P$ and $Q$ is defined by $d(P, Q)=\min _{R, \mathbf{a}} d(P, Q, R, \mathbf{a})$. Although complicated as it might appear, the optimal rotation matrix and translation vector can be found simultaneously in $O(n)$ time. Schwartz [20] showed that $d(P, Q, R, \mathbf{a})$ is minimized when $\mathbf{a}=0$ and

$$
\begin{equation*}
R=\left(A^{t} A\right)^{\frac{1}{2}} A^{-1} \tag{2}
\end{equation*}
$$

where the matrix $A=\left(A_{i j}\right) i, j=1,2,3$ is given by

$$
\begin{equation*}
A_{i j}=\sum_{k=1}^{n}\left(p_{k}\right)_{i}\left(q_{k}\right)_{j} \tag{3}
\end{equation*}
$$

where $A^{\frac{1}{2}}=B$ means $B B=A$, and $\mathbf{o}$ denotes the zero vector. Thus, $d(P, Q), R$ and a can be computed in $O(n)$ time [17].
We adopt Martin's ProFit package (standing for protein fitting system) [16] to calculate the rmsd between C- $\alpha$ atoms of paired protein backbones. ProFit has many features including flexible specification of fitting zones and atoms, calculation of RMS over different zones or atoms, RMS-byresidue calculation. Fitting was performed using the McLachlan algorithm [17].

### 2.2 Euler's Rotation Theorem

According to Euler's rotation theorem [13] , any rotation can about the origin point be described by using three angles. The rotation is determined by 3 consecutive rotations with 3 Euler angles $\left(\theta, \beta^{\prime}, \gamma^{\prime}\right)$. The first rotation is done by the angle $\theta$ ( $=\sin ^{-1} \alpha$ ) around the $z$-axis, the second is done by the angle $\beta^{\prime}(=\beta \pi)$ around the $x$-axis, and the third rotation is done by the angle $\gamma^{\prime}$ around the $z$-axis.
As a result, we reduce the problem of finding a good rotation matrix to the new problem of finding a good 3 -parameter. The rotation matrix is thus characterized by just adjusting the 3 uniformly distributed parameters.

### 2.3 Our Rotation Matrix

our 3-parameter method $(\alpha, \beta, \gamma)$ can be summarized as the following:

## - Rotation around $x$-axis:

Given a unit vector $\mathbf{p}=(x, y, z)^{T}, \mathbf{p}$ is transformed into $\mathbf{p}^{\prime}$ by a rotation around the $x$-axis by angle $\sin ^{-1} \alpha=\theta$. That is, let

$$
\mathbf{p}^{\prime}=\left(\begin{array}{l}
x_{\alpha} \\
y_{\alpha} \\
z_{\alpha}
\end{array}\right)=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \sqrt{1-\alpha^{2}} & -\alpha \\
0 & \alpha & \sqrt{1-\alpha^{2}}
\end{array}\right] \cdot \mathbf{p}
$$

Since $\sin \theta=\alpha$ and thus, $\cos \theta=\sqrt{1-\alpha^{2}}$.

## - Rotation around $z$-axis:

The vector, $\mathbf{p}^{\prime}=\left(x_{\alpha}, y_{\alpha}, z_{\alpha}\right)^{T}$, is transformed into the probe $\mathbf{p}^{\prime \prime}$ by a rotation around the $z$ axis by angle $\beta \pi$. That is, let
$\mathbf{p}^{\prime \prime}=\left(\begin{array}{c}x_{\beta} \\ y_{\beta} \\ z_{\beta}\end{array}\right)=\left[\begin{array}{ccc}\cos \beta \pi & -\sin \beta \pi & 0 \\ \sin \beta \pi & \cos \beta \pi & 0 \\ 0 & 0 & 1\end{array}\right] \cdot \mathbf{p}^{\prime}$ then we will get new coordinate of $\left(x_{\beta}, y_{\beta}, z_{\beta}\right)^{T}$.

```
\(\operatorname{Struc-Align}\left(P, Q, \alpha_{I}, \beta_{I}, \gamma_{I}, \mathbf{p}\right)\)
Input: Two set of 3D coordinates of points \(P=\left\{p_{1}, p_{2}, \ldots, p_{n}\right\}\) and \(Q=\left\{q_{1}, q_{2}, \ldots, q_{m}\right\} ; n<m\).
    The \(\alpha_{I}, \beta_{I}\) and \(\gamma_{I}\) are real numbers that are between -1 to 1 .
    \(\triangleright\) These inputs control the initial position of 3 parameters box and affect the explored area.
    \(\triangleright \mathbf{p}\) is the vector \((x, y, z)^{T}\), explained in section 2.1.
Output: \((s, \alpha, \beta, \gamma)\) is a sufficiently low RmsD \(s\) and \((\alpha, \beta, \gamma)\).
    \(\triangleright(\alpha, \beta, \gamma)\) is the best position of 3 parameters box.
Global : \(T, t, F, \alpha_{\max }, \beta_{\max }, \gamma_{\max }\).
        The threshold \(T\) and \(F\) are both integer numbers.
            \(\triangleright T\) is total trial number of perturbation.
            \(\triangleright t\) is the count that records the number of perturbation carried out so far.
            \(\triangleright F\) is the maximum number of consecutive failed perturbations for a probe to restart.
        \(\alpha_{\max }, \beta_{\max }, \gamma_{\max }\) are real numbers between 0 to 1 .
        \(\triangleright\) These inputs control the range of parameters perturbation variances.
    \((\alpha, \beta, \gamma) \leftarrow\left(\alpha_{s}, \beta_{s}, \gamma_{s}\right) \leftarrow\left(\alpha_{I}, \beta_{I}, \gamma_{I}\right)\).
    \(Q^{\prime} \leftarrow \operatorname{Trans}(Q, \operatorname{Rot}-\mathrm{m}(\alpha, \beta, \gamma, \mathbf{p})) . \quad \triangleright Q^{\prime}\) is a temp array of atoms set of protein.
    \(L \leftarrow \operatorname{Mbm}\left(P, Q^{\prime}\right) ;(R, \mathbf{a}) \leftarrow \operatorname{Ms-Fit}\left(L, P, Q^{\prime}\right) ; s \leftarrow \operatorname{RMSD}\left(P, Q^{\prime}, R, \mathbf{a}\right)\).
    \(f \leftarrow 0 . \quad \triangleright\) Initializing the counter.
    while \(t \leq T\) do
        \(\left(\alpha^{\prime}, \beta^{\prime}, \gamma^{\prime}\right) \leftarrow \operatorname{Perturb}(\alpha, \beta, \gamma)\).
        \(Q^{\prime} \leftarrow \operatorname{Trans}\left(Q, \operatorname{Rot}-\mathrm{m}\left(\alpha^{\prime}, \beta^{\prime}, \gamma^{\prime}, \mathbf{p}\right)\right) . \quad \triangleright Q^{\prime}\) is a temp array of atoms set of protein.
        \(L \leftarrow \operatorname{MBm}\left(P, Q^{\prime}\right) ;(R, \mathbf{a}) \leftarrow \operatorname{Ms-Fit}\left(L, P, Q^{\prime}\right) ; s^{\prime} \leftarrow \operatorname{Rmsd}\left(P, Q^{\prime}, R, \mathbf{a}\right)\).
        if \(s^{\prime} \leq s\) then \(s \leftarrow s^{\prime} ;(\alpha, \beta, \gamma) \leftarrow\left(\alpha_{s}, \beta_{s}, \gamma_{s}\right) \leftarrow\left(\alpha^{\prime}, \beta^{\prime}, \gamma^{\prime}\right) ; f \leftarrow 0 ;\)
                    else \(f \leftarrow f+1\)
        if \(f \geq F\) then return \(\left(s, \alpha_{s}, \beta_{s}, \gamma_{s}\right)\).
        \(t \leftarrow t+1\).
    return \(\left(s, \alpha_{s}, \beta_{s}, \gamma_{s}\right)\).
```

$\operatorname{MBM}(P, Q)$ returns the minimum bipartite matching of two point sets $P$ and $Q$.
$\operatorname{Perturb}(\alpha, \beta, \gamma)$.
Input: The $\alpha, \beta$ and $\gamma$ are real numbers between -1 to 1 .
$\Delta$ These inputs control the present position of 3 parameters box and affect the explore area.
Output: 3 real numbers ( $\alpha^{\prime}, \beta^{\prime}, \gamma^{\prime}$ ).
$\triangleright$ These outputs are the new position of 3 parameters box.

```
\Delta\alpha\leftarrowRAND}(-\mp@subsup{\alpha}{\operatorname{max}}{},\mp@subsup{\alpha}{\operatorname{max}}{});\Delta\beta\leftarrow\operatorname{RaND}(-\mp@subsup{\beta}{\operatorname{max}}{},\mp@subsup{\beta}{\operatorname{max}}{});\Delta\gamma\leftarrow\operatorname{RAND}(-\mp@subsup{\gamma}{\operatorname{max}}{},\mp@subsup{\gamma}{\operatorname{max}}{})
\alpha
return ( }\mp@subsup{\alpha}{}{\prime},\mp@subsup{\beta}{}{\prime},\mp@subsup{\gamma}{}{\prime})
```

$\operatorname{RAND}(a, b)$ is a random function returning a real number uniformly distributed between $a$ and $b$.
$\operatorname{BACK}(\alpha)=\left\{\begin{array}{rcl}-2-\alpha & \text { if } & \alpha \leq-1 \\ 2-\alpha & \text { if } & \alpha \geq 1 \\ \alpha & \text { otherwise } & \quad ; \operatorname{Round}(\theta)=\left\{\begin{array}{rll}2+\theta & \text { if } & \theta \leq-1 \\ -2+\theta & \text { if } & \theta \geq 1 \\ \theta & \text { otherwise }\end{array}\right.\end{array}\right.$
Trans $(A, R)$.
Input: $A$ is an array of 3D points with size $n$. $R$ is the rotation matrix.
Output: An array of 3D points, $B$.

```
    for \(i \leftarrow 1\) to \(n\) do
    \(B[i] \leftarrow R \cdot A[i] \quad \triangleright B\) is the array containing the transformed \(n\) points.
    return \(B\).
```

Figure 1: Aligning two sets of atoms with low rmsd by pairing points according to the minimum bipartite matching measurement


Figure 2: Three parameters $(\alpha, \beta, \gamma)$, or angles $\left(\sin ^{-1} \alpha, \beta \pi, \gamma \pi\right)$, suffice to determine a rigid 3D rotation of points about origin.

## - Rotation around the probe $\mathrm{p}^{\prime \prime}$ :

The last rotation matrix, $R_{\gamma}$, do the body rotation around the probe $\mathbf{p}^{\prime \prime}$ by angle $\gamma \pi$; see [8] for related discussions about the transformation. That is, let

$$
\begin{aligned}
& (x, y, z)=\left(x_{\beta}, y_{\beta}, z_{\beta}\right)^{T} \\
& c=\cos \gamma \pi, s=\sin \gamma \pi, h=1-c \\
& R_{\gamma}=\left[\begin{array}{ccc}
c+x^{2} h & x y h-z s & x z h+y s \\
x y h+z s & c+y^{2} h & y z h-x s \\
x z h-y s & y z h+x s & c-z^{2} h
\end{array}\right]
\end{aligned}
$$

### 2.4 Minimum Bipartite Matching

There are several proposed algorithms for the minimum bipartite matching problem; sometimes it is also referred as the assignment problem. Here we adopted the Munkres [18, 2, 1, 19] algorithm. The public available implementation is written with Perl language. To improve the efficiency of computation, we implement the Munkres algorithm and write hundreds lines of C Codes, and and the produced codes are strictly verified by comparing the results with the public Perl package.

### 2.5 Perturb

Note that the methodology of the current system is generally a randomized algorithm and a variable, Perturb algorithm and $F$. The performance of Perturb algorithm is depended on various setting of 3-parameter, $\alpha_{\max }, \beta_{\max }, \gamma_{\max }$. The perturb algorithm is displayed in figure 1.

## 3 The Experiment for Three Parameters

In order to obtain the suitable 3-parameters, we select 50 samples of 6,000 samples, and carry following experiments to find out good parameters of the our programs.

The experiments can help us to analyze how the 3 -parameter, $\alpha_{\max }, \beta_{\max }, \gamma_{\max }$, affects the final rmsd. The better $\alpha_{\max }, \beta_{\max }$, and $\gamma_{\max }$ are found. We have to assume that $T$ is 50 , and $F$ is 11 . The other two parameters of 3 parameters have to be set to 0.2 . For example, if we want to search a good $\alpha_{\max }$, we must set $\beta_{\max }=\gamma_{\max }=0.2$ and so on.

Then, We start to performance the experiment. First, we test a good $\alpha_{\max }$ among $0.2,0.4,0.6,0.8$, and 1. Secondly, we use uniformly distributed method to divide the two neighbors of the maximal result into six number and test the six numbers. For example, the maximum result is 0.4 , and its neighbors are 0.2 and 0.6 . We have to test $0.25,0.3,0.35,0.45,0.5$, and 0.55 . Thirdly, in last step we can find another maximal result from the six value. We use uniformly distributed method to divide the two neighbors of the maximal result into two numbers. For example, if the maximal result is 0.45 , we can get 0.425 and 0.475 . Last of all, we test the two value and choose maximal result for our final parameter. After these experiments we find a good 3-parameter, $\left(\alpha_{\max }, \beta_{\max }, \gamma_{\max }\right)=(0.475,0.2,0.2)$, and the results are shown in Figure 3 and Figure 4.

Furthermore, we have another experiment. We try to analyze how the variable, $F$, affects the final $r m s d$. We set $T=50$, and then we test $F$ between $\frac{1}{2} \sqrt{T}$ and $2 \sqrt{T}$ by experience. Now $F$ which we test is from 3 to 15 . Under the good 3-parameters, $\left(\alpha_{\max }, \beta_{\max }, \gamma_{\max }\right)=(0.475,0.2,0.2)$, we find that the good value of $F$ is 13 and the results are shown in Figure 4.

## 4 The Pretest Algorithm

The main idea for the pretest algorithm is to save the computer times in the finite resource. We have only finite resource to get the best effect. Therefore, we develop the Pretest Algorithm. The main concept of pretest algorithm is to filter the fitting parameters for our programs. We can use the algorithm to find a initial alignment from the


Figure 3: The Experimental improvement ratios under different $\alpha_{\max }$ and $\beta_{\max }$, and fix the other parameters.


Figure 4: The Experimental improvement ratios under different $\gamma_{\max }$ and $F$, and fix the other parameters.

```
Align-TOR-K \(\left(P, Q, T, F, \alpha_{\max }, \beta_{\max }, \gamma_{\max }, T O R, K\right)\)
Input: The \(\left(P, Q, T, F, \alpha_{\max }, \beta_{\max }, \gamma_{\max }\right)\) parameters are explained in figure 1.
\(T O R\) is a real number representing the \(r m s d\) threshold for the pretesting phase.
\(K\) is a integer that control the maximum number of failed perturbations.
Output: \((s, L)\)
    \(s \leftarrow \infty ; \mathbf{p} \leftarrow(0,1,0)^{T}\).
    while \(t \leq T\) do
            \(\alpha \leftarrow \operatorname{Rand}(-1,1) ; \beta \leftarrow \operatorname{RAND}(-1,1) ; \gamma \leftarrow \operatorname{RanD}(-1,1) ; k \leftarrow 0\).
                \(\triangleright(\alpha, \beta, \gamma)\) are uniformly distributed random values ranged in \((-1,1)\).
            while \(k \leq K\) do
                \(\left(\alpha^{\prime}, \beta^{\prime}, \gamma^{\prime}\right) \leftarrow \operatorname{Perturb}(\alpha, \beta, \gamma)\).
                \(Q^{\prime} \leftarrow \operatorname{Trans}\left(Q\right.\), Rot-m \(\left.\left(\alpha^{\prime}, \beta^{\prime}, \gamma^{\prime}, \mathbf{p}\right)\right) . \quad \triangleright Q^{\prime}\) is a temp array of atoms set of protein.
                    \(L \leftarrow \operatorname{MBm}\left(P, Q^{\prime}\right) ;(R, \mathbf{a}) \leftarrow \operatorname{Ms-Fit}\left(L, P, Q^{\prime}\right) ; s^{\prime} \leftarrow \operatorname{RMSD}\left(P, Q^{\prime}, R, \mathbf{a}\right)\).
                    if \(s^{\prime} \leq T O R \cdot s\) then \(\left(s^{\prime}, \alpha_{s}^{\prime}, \beta_{s}^{\prime}, \gamma_{s}^{\prime}\right) \leftarrow \operatorname{Struc}-\operatorname{Align}(P, Q, \alpha, \beta, \gamma, \mathbf{p}) ; k \leftarrow K\).
                    \(k \leftarrow k+1 ; t \leftarrow t+1\).
            if \(s^{\prime} \leq s\) then \(s \leftarrow s^{\prime} ;\left(\alpha_{s}, \beta_{s}, \gamma_{s}\right) \leftarrow\left(\alpha_{s}^{\prime}, \beta_{s}^{\prime}, \gamma_{s}^{\prime}\right)\).
    \(Q^{\prime} \leftarrow \operatorname{Trans}\left(Q\right.\), Rot-m \(\left.\left(\alpha_{s}, \beta_{s}, \gamma_{s}, \mathbf{p}\right)\right) . \quad \triangleright Q^{\prime}\) is a temp array of atoms set of protein.
    \(L \leftarrow \operatorname{MBm}\left(P, Q^{\prime}\right) . \quad \triangleright L\) is the matching list of point sets \(P\) and \(Q\).
    return \((s, L)\).
```

Figure 5: The pretest algorithm can try to filter the fitting parameters for our programs. We can use the algorithm to find a initial alignment for protein pairings.
protein pairings, and we use two thresholds, TOR and K, to filter the possible candidate parameters. TOR is a real number to represent the rmsd threshold for the pretesting phase. K is a integer that control the maximum number of failed perturbations. We give the program K times to find a RMSD value which must satisfy the following condition

$$
s^{\prime} / s \leq T O R
$$

, where $s$ is the minimal rmsd which we find in this time and $s$ ' is the value which we find under the k times testing. If the s ' is ok, we use this parameters to run our program and give it more resource to find a better result. By the way, we can save a lot of resources to find a good alignment.

## 5 Experimental Result

In this section, we show the experimental methods and result between CE methods and our previous methods. First of all, we illustrate what samples we use for our experiments, and then we explain that the samples in VAST are different from the one in CE. Secondly, we analyze the improvement ratios of our method tested on the given data. In the third part, we display and analyze the experimental results about our Pretest algorithms, CE and VAST. Finally, we analyze the experimental execution time of our programs for some different conditions.

### 5.1 Sample Source

In our previous experiment, We choose the PDB for our experimental sample source, and we randomly pick 200 protein structures in the PDB database as our experimental subjects by the uniform distribution sampling. For each chosen protein structures We randomly choose 30 structure alignments listed on the database of VAST as the tested targets. Totally, there are 6,000 protein pairings tested by our previous experiment. We use the term, PA, to stand for one of the 200 randomly picked protein structures, and we use PB to stand for one of the 30 neighbors of each PA. we randomly get the three parameters for our methods to compare with the VAST methods. The sample distribution is showed in Figure 6. We illustrate the number of $\mathrm{C}-\alpha$ atoms of PA , the number of protein pairings and the average of improved ratio, at Figure 7. The result which we improve against the VAST is $9.29 \%$.

We want to use the same samples to test the CE method. But we find that the alignments sought out by CE are different from the ones by VAST. The CE programs always find out its own alignments, and we can not assign the number of

C- $\alpha$ for our experiments. In this situation, the VAST and the CE can not be compared for each other. Therefore, we can only compare the results between our methods and the CE methods. We divide the process which we get the new protein pairings into several parts. First, we use the 6,000 protein pairings from VAST for our original samples. We input each pairings into the CE programs, and the new protein pairings are outputted. We use the aligned atoms from PA we input for our new PA, and the PB is the same as which we input. We call the new PA, ce-PA. We use the pairings of ce-PA and PB for our new sample pairings. The relation between the number of $\mathrm{C}-\alpha$ atoms of ce-PA and the number of protein pairs are illustrated at Figure 8.

### 5.2 The Experimental Result With CE

Now we have 6,000 new protein pairings for our experiment. We use the better three parameter, ( $0.475,0.2,0.2$ ), to execute the Struc-align algorithm. We first measures each sample pairings by calculating its original alignment's rmsd value. The measurement is confirmed and double checked wich the rmsd by the PROFIT package kits [16].

After we finish the 6,000 samples, the results note that we can improves almost every sampled CE pairs. By the ascending order on the number of $\mathrm{C}-\alpha$ atoms of ce-PA, we partition the samples into 40 points, with each point standing for 150 protein pairs. Figure 9 shows the relation between the number of $\mathrm{C}-\alpha$ atoms of PA and the improvement ratios contrast to the given VAST alignment. The formula of the improvement ratio is defined by

$$
\rho=(A-B) / A,
$$

where $A$ is the original $r m s d$ value by the CE alignment, while $B$ is improved(smaller) $r m s d$ value by our structure alignment method. The improvement ratios of our samples are mostly distributed from $8 \%$ to $15 \%$. As a total, the average of the improvement ratios is $11.03 \%$.

The execution time of the experiment for our method is summarized in Figure 10, which shows the relation between the number of $\mathrm{C}-\alpha$ atoms of ce-PA and the execution time (CPU processor time) of our structure alignment system needed for the samples to run. Note that each drawn point in Figure 10 represents a group of 150 protein pairs.
The structure alignment system is implemented and tested under the Linux Red Hat 4.0 system. Each of the experimental machine is equipped with $\operatorname{Intel}(\mathrm{R})$ Pentium(R) 4 CPU 3.00 GHz processor and 2GB RAM main memory. The experiment takes approximately 100 hours to finish the experiment on the total 6,000 protein structure


Figure 6: The distribution of the 200 randomly picked protein structures in PDB and their 30 neighbor structures. The total number of protein pairs is 6,000 .

| The number <br> of C- $\alpha$ <br> atoms of PA | The number <br> of protein <br> pairings | The average <br> of improved <br> ratio (\%) | The average <br> of execution <br> time $(S e c)$ | The standard <br> deviation of <br> improved ratio (\%) | The standard <br> deviation of <br> execution time $(S e c)$ |
| :---: | :---: | ---: | ---: | ---: | ---: |
| $50<$ | 1541 | 7.61 | 0.57 | 11.99 | 1.27 |
| $50-100$ | 1586 | 7.17 | 5.98 | 11.98 | 5.54 |
| $100-150$ | 1030 | 8.42 | 15.16 | 12.48 | 14.83 |
| $150-200$ | 674 | 14.71 | 41.73 | 15.61 | 41.49 |
| $200-250$ | 469 | 11.30 | 161.01 | 14.74 | 160.92 |
| $250-300$ | 404 | 9.57 | 401.65 | 15.07 | 401.90 |
| $300-350$ | 186 | 17.57 | 873.34 | 18.21 | 875.59 |
| $350-400$ | 40 | 12.66 | 1592.63 | 25.30 | 1612.83 |
| $400>$ | 70 | 15.67 | 10315.05 | 21.41 | 10389.45 |
| Total | 6000 | 9.29 | 206.68 | 13.22 | 206.26 |

Figure 7: The result is to execute the previous algorithm with random parameters and compare with the VAST. The distribution of our experimental data containing the number of $\mathrm{C}-\alpha$ atoms of PA, the number of protein pairings, the average of improved ratio, the average of execution time,the standard deviation of improved ratio and the standard deviation of execution time.


Figure 8: The distribution of the new sample pairings. The total number of protein pairs is 6,000 .


Figure 9: The improvement ratios opposite to the rmsd of the CE alignment. The improvement ratios are mostly distributed from $8 \%$ to $15 \%$. The average is $11.03 \%$. Each point stands for 150 sample pairings.
pairings. The Figure 11 is the result which we compare against the CE, and the average of improved ratio is $11.03 \%$.

### 5.3 The Experimental Result With CE for Pretest Algorithm

We execute the pretest algorithm for our experiment.First, we have to set the other parameters. The parameters for us to execute this experiment is $T=330, F=8, \alpha=0.35, \beta=0.1, \gamma=0.18$. We give the TOR for 1.23 and the K for 1 to run the 6,000 data. We also use the same ce-PA to run the program. Our program can find a alignment. We compared the value of RMSD between our alignment and the CE alignment. In this comparison, our program is $6.93 \%$ more than the CE. The execution time for the program is shoed in Figure 14. We have finished the 4,445 protein pairings, but the time we have to spend on the other 1,555 is for a long time. To date, we continue to run them.

The distribution for the improvement ratio is showed in Figure 13. When the number of atom for ce-PA is less than 100, we almost find a better alignment than the CE. But the result is not good if the ce-PA is more than 100 . This experiment can indicate that we can find a better value about TOR and K to have better alignment. The improvement ratios opposite to the rmsd of the CE alignment. The improvement ratios are mostly greater than 0 . The average is $6.93 \%$. The execution time for the program is shoed in Figure 14. The experimental result is showed in Figure 12.

## 6 Conclusion and Future Work

Bioinformatics has become an essential tool not only to basic research but also to serious research


Figure 10: The execution time of our structure alignment system with better parameters needed for the samples to run. Each point stands for 150 sample pairings.
in biotechnology and biomedical sciences. Currently, the field is under enormous expansion and witnessed by the dramatic increase in the number of related bioinformatic literatures.

In this paper, we use the algorithms which we proposed previous to improve the rmsd value between protein structure pairings by finding better alignment list. We use a set of experiments to test the parameters. We apply the tested parameters to run the experiment results. Our method with better parameters can improves the alignment computed by the CE package and the average of improvement ratios is $11.03 \%$. Therefore, the system demonstrates that the method with 3D Euclidean distance, minimum bipartite matching and perturbed parametric searching scheme indeed improves existed known system like the VAST and the CE. It is interesting to know what is the best parameter for our method. We can use another better one to find them.

We use the pretest algorithm to test the protein pairings without initial alignment. We can find the better alignments than the CE. We can have another better method to find the initial alignment for the global alignments. The average which our result can have is $6.93 \%$ more than the result of CE. Our methods need the better parameters to have the better results. We can continue to test them. Besides, we can use our program to classify the protein and fine the similarity about all proteins.

Furthermore, since the structure comparison problem, like many scientific computation/simulation problem, is very time-consuming under cases of large structures and large number of paired structures, it is desirable to implement the system under massive parallel machines cluster, e.g., the grid-environment, to increase the throughput of the system.

| The number <br> of C- $\alpha$ <br> atoms of PA | The number <br> of protein <br> pairings | The average <br> of improved <br> ratio (\%) | The average <br> of execution <br> time $(S e c)$ | The standard <br> deviation of <br> improved ratio (\%) | The standard <br> deviation of |
| :---: | :---: | ---: | ---: | ---: | ---: |
| $50<$ | 682 | 12.23 | 0.10 | 10.41 | execution time $(S e c)$ |
| $50-100$ | 2208 | 14.18 | 1.01 | 9.61 | 0.09 |
| $100-150$ | 1150 | 9.50 | 5.50 | 7.13 | 0.68 |
| $150-200$ | 768 | 8.55 | 20.79 | 7.22 | 2.98 |
| $200-250$ | 489 | 8.16 | 50.19 | 6.77 | 9.51 |
| $250-300$ | 450 | 7.62 | 96.73 | 7.31 | 13.99 |
| $300-350$ | 160 | 7.40 | 220.59 | 7.74 | 39.29 |
| $350-400$ | 31 | 4.55 | 349.58 | 4.46 | 61.52 |
| $400>$ | 62 | 5.02 | 2772.87 | 3.58 | 54.06 |
| Total | 6000 | 11.03 | 51.79 | 8.93 | 1602.22 |

Figure 11: The result is to execute the previous algorithm with tested parameters and compare with the CE . The distribution of our experimental data containing the number of $\mathrm{C}-\alpha$ atoms of ce-PA, the number of protein pairings, the average of improved ratio, the average of execution time, the standard deviation of improved ratio and the standard deviation of execution time.

| The number <br> of C- $\alpha$ <br> atoms of PA | The number <br> of protein <br> pairings | The average <br> of improved <br> ratio (\%) | The average <br> of execution <br> time $(S e c)$ | The standard <br> deviation of | The standard <br> deviation of |
| :---: | :---: | ---: | ---: | ---: | ---: |
| $20<$ | 57 | 6.29 | 0.37 | 19.4 | 0.95 |
| $20-40$ | 360 | 12.57 | 1.12 | 18.6 | 0.62 |
| $40-60$ | 828 | 16.48 | 5.59 | 16.9 | 2.98 |
| $60-80$ | 899 | 14.56 | 15.04 | 18.08 | 20.08 |
| $80-100$ | 697 | 5.35 | 37.06 | 23.52 | 32.61 |
| $100-120$ | 548 | -0.15 | 69.52 | 32.39 | 35.25 |
| $120-140$ | 430 | -3.72 | 141.87 | 36.76 | 119.08 |
| $140-160$ | 282 | -1.93 | 370.67 | 19.61 | 232.55 |
| $160-180$ | 306 | -8.31 | 600.71 | 31.09 | 306.28 |
| $180-200$ | 31 | 5.14 | 1669.88 | 19.72 | 477.24 |
| $200>$ | 7 | 9.05 | 2625.85 | 6.88 | 980.68 |
| total | 4445 | 6.93 | 112.93 | 25.72 | 261.52 |

Figure 12: The result is to execute the pretest algorithm and compare with the CE. The distribution of our experimental data containing the number of $\mathrm{C}-\alpha$ atoms of ce-PA, the number of protein pairings, the average of improved ratio, the average of execution time, the standard deviation of improved ratio and the standard deviation of execution time.


Figure 13: Our pretest algorithm opposite to the rmsd of the CE alignment. The improvement ratios are mostly greater than 0 . The average is $6.93 \%$. Each point stands for 150 sample pairings.

There is an important direction of research about the topic of protein structure alignment. The problem of local structure alignment is to find the functional (or active) part of a given query protein; these active parts imply a substructure similarity between two proteins. The problem of identification of the similar substructure of a protein pair will indeed be a challenge.

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Figure 14: The execution time of our pretest algorithm and structure alignment system needed for the samples to run. Each point stands for 150 sample pairings.

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