

## An Efficient Learning Model for Mobile Environments using Graph and Probability Analysis

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### *Abstract*

In this paper, our approach uses two views in modeling: the physical view and the logical view. In the physical view, we consider and model the link reliability (communication links), Multi-access Probability (the access problems), moving patterns (user's learning behavior), and data allocations (location management) in the mobile learning environment. In the logical view, we consider and model the course planning strategy to find the suitable way for a learner to learn a particular curriculum (consists of courseware units). A course planning scheme is to suggest a learning sequence. Numerical examples are given to enumerate the proposed approach.

### **1. Introduction.**

In general, learning involves learning the things that we do not understand. In the knowledge exploding modern society, we find that learning is not merely restricted to the classroom, but technology has enabled us to extend beyond classroom boundaries. Besides traditional face-to-face teaching, the introduction of networks, both wired and wireless, has enabled new forms or channels for learning such as remote learning and e-learning.

Recently, wireless networks have become extremely popular, with access points becoming available at phenomenal rates. Mobile users are now able to demand access to content almost anywhere they want. The recent proliferation of mobile devices has increased such demand. These mobile devices (such as mobile phones and PDAs) are becoming increasingly powerful enough to handle multimedia data. Wireless networks such as GPRS and GSM are also beginning to support higher transmission rates, thus making them ideal mediums for multimedia data transmission. GSM supports wireless voice and digital services. GPRS supports non-voice services

over cellular networks. Both networks come with rich features for such services and applications making them potential distribution mediums for multimedia services such as voice, video, multimedia on demand, video conferencing and mobile Internet, supporting data rates of up to 2mbps [1].

Technology in recent years has contributed much to the rise of e-learning and the introduction of new forms of teaching and learning. The use of multimedia and the introduction of high-speed networks have only enhanced e-learning channels. The recent popularization of wireless networks and the proliferation of mobile devices have extended the possibility of e-learning to users of mobile devices, thus creating several opportunities for investigation in this area.

The potential mobile users create several opportunities for mobile e-learning. While mobile e-learning is not new and has been in practice in the US defense for many years, it has been proved to be the most efficient and most economical cost learning patterns. There are several governmental organizations implementing similar strategies. The potential for mobile e-learning will be extremely vast once the underlying infrastructure can unleash its potential. Access to information immediately and on-demand will be an evermore important requirement for users of mobile devices. This also applies to the mobile e-learning arena.

When the courseware unit capability indicators (We will mention it in section 4.1) have been transferred into a directed graph, we apply the minimum weight branching algorithm to find the learning sequence based on the imposed requirements. The purpose of "minimum weight branching" is to find an efficient learning path from a directed graph. The arrows in directed graph are capability indicator relations (Logical view in Figure 1). The outcome of the learning sequence once minimum weight branching has been applied is mapped (the arrows pass through Logical

Physical border in Figure 1) to the physical network environment using the data allocation scheme.

Figure 3 shows that the idea of mapping logical courseware unit into a physical network environment.

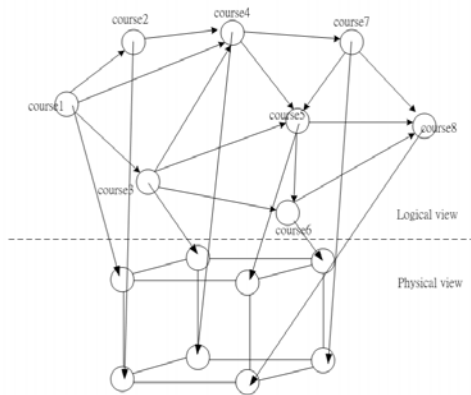


Figure 1: Map the course to physical network

In section 4.2, we will present how we solve the course planning problem.

## 2. Related work.

Several related research work [2] discusses the architecture of mobile-learning environments. The architecture of mobile learning environments is concerned with the development of the standards, and providing interoperability among heterogeneous systems and learning object reuse. Based on the standardization work, they propose open and distributed architectures that identify some common services (e.g. software service) for e-learning domains. Some mobile learning architecture has also integrated digital content topics in hybrid learning environments [3]. These research projects are concerned about digital representation such as three dimensional graphics and advanced animation techniques. They conduct analysis on the possibility of content that might be able to imitate or to substitute the teachers' human existence itself.

Other related works focus their efforts on e-learning theories. Like constructivist values for web-based instruction [4, 5]. In these research projects, their attempts are focused on trying to do convert traditional (face-to-face) courses to multimedia web-based courses. They focus on ways to encourage interactive learning and the use of motivational strategies. In their experiments, they train students using digital course and video tapes of an instructor answering questions and discussing course content. In another theory, role-base learning theory, they focus on familiarizing students with intellectual frameworks and establishing principles and general approaches. Our research focuses on the course planning scheme and formulate the successful

rate on the network when a mobile learner requires a courseware unit.

## 3. Physical View.

The Physical View is concerned with network reliability. This is an important consideration when allocating resources in such an environment. We discuss the physical aspects of mobile environments such as 3G networks and discuss the important properties related to mobile learning such as link probability, Multi-access Probability.

### 3.1 Link Probability.

Link probability deals with the quantization of communication links to determine network reliability. In link probability, the initial transfer reliability is formulated and from this, a simple linear regression model is used to get the approximate dynamic probability.  $TR(e_i)$ :The initial transfer reliability of link at traffic load=0.  $PR(e_i,r)$ :The probability of the link  $e_i$  can work well at traffic ratio  $r$  ( $r$  = traffic load/link capacity).  $PR(e_i,r)=(B_0+B_1 \times r) \times TR(e_i)$  where  $B_0$  and  $B_1$  are shown in the Table 1.

Table 1: Link probability

Ratio	0.0-0.2		0.2-0.4		0.4-0.6		0.6-0.8		0.8-1.0	
Coef	B0	B1	B0	B1	B0	B1	B0	B1	B0	B1
	1.23	-1.17	1.28	-1.08	1.35	-1.01	1.43	-0.96	1.50	-0.89

### 3.2. Multi-access Probability.

Multi-access-reliability involves formulating access for multiple data (courseware unit). After a request is sent by a user, the material provider may need to send several resources back. The access time of these resources may not be equal. The following formula is the definition of Multi-access Probability for User<sub>i</sub>.  $M_1, M_2, \dots, M_n$  are the required resources.

$$R(U_i | M_1, \dots, M_n) = R(U_i | M_1) + (1 - R(U_i | M_1)) \times R(U_i | M_2) + \dots + (1 - R(U_i | M_{n-1}))^n \times R(U_i | M_n)$$

$$= R(U_i | M_1) \left\{ \sum_{k=0}^n (1 - R(U_i | M_k))^k \right\}$$

where  $n$  is total number of required courseware

Here we give an example as shown in Figure 2. In the following examples, we have four nodes. If every physical link probability is 0.9. A user in  $V_3$  requires  $M_1, M_2$ . The successful ratio to obtain  $M_1$  and  $M_2$  is  $R(U_i | M_1, M_2) = 0.9 \times 0.9 + (1 - 0.9 \times 0.9) \times 0.9 \times 0.9 = 0.972$ .

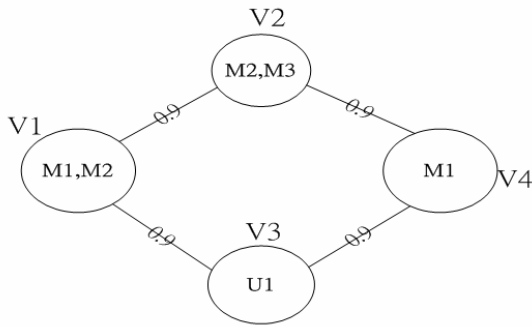


Figure 2: Four node example

### 3.3 Moving patterns.

Moving patterns record users' behaviors. This is achieved by using a method to mine the moving patterns from the previous data log. With the moving patterns, we can develop a data allocation scheme for proper allocation of personal and shared data. Table 2 and Table 3 are Moving frequency matrix and Transition probability matrix. Moving frequency matrix is used to recorded user's behaviors. The Transition probability matrix is used to improve data allocation scheme.

Table 2: Moving frequency matrix

count	V1	V2	v3	v4
V1v2	200	0	0	300
V1v3	250	0	0	250
V2v1	0	300	200	0
V2v4	0	100	400	0
V3v1	0	150	350	0
V3v4	0	450	50	0
V4v2	250	0	0	250
v4v3	350	0	0	150

Table 3: Transition Probability Matrix

P <sub>i,j,k,t</sub>	V1	V2	v3	v4
V1v2	0.4	0	0	0.6
V1v3	0.5	0	0	0.5
V2v1	0	0.6	0.4	0
V2v4	0	0.2	0.8	0
V3v1	0	0.3	0.7	0
V3v4	0	0.9	0.1	0
V4v2	0.5	0	0	0.5
v4v3	0.7	0	0	0.3

Since we take into account the probability that user may move from his current node to neighbor

nodes, we must use the summation of the product of the static remote media access probability of the neighbor node and its transition probability to represent the remote media access probability for the mobile environment. The RMAP is Remote Media Access Probability which formulates a remote user access the required courseware using the concept of moving patterns.

$$RMAP(U) = \sum_j ((P_{i,j,k,t}) \times RMAP(N_j))$$

Suppose the following:

In Figure 3, Assume user 1 came from E, and is now at F now. He needs media M1, M2, and M3 for his learning mission.

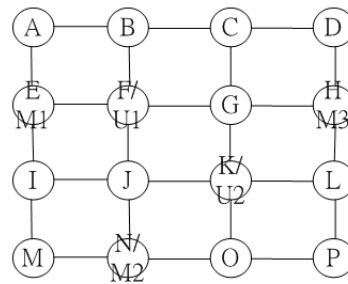


Figure 3: RMAP pattern

We need to compute the remote media access probability RMAP(F). And suppose that the transition probability from EF to neighbors B,E,G,J are 0.2,0.3,0.3,0.2 respectively. Then RMAP(F) is formulated as follows.

$$RMAP(U1) = 0.2 \times RMAP(B) + 0.3 \times RMAP(E) + 0.3 \times RMAP(G) + 0.2 \times RMAP(J)$$

### 3.4 Data Allocation.

Distributed multimedia applications have played an important role in the recent advances in mobile learning environments. In such environments, storage volume can be quite large and as a result, we need to find a way to allocate courseware unit to improve the learning efficiency. Data allocation improves access reliability to the courseware units. The purpose of this is to find a way to allocate the course material appropriately in a real network environment. From this, we can provide a higher standard of service to subscribers. In Figure 4, the DMDB network is physical network and we use our data allocation scheme to allocate courseware into the physical network. The Data allocation strategy is as follows.

We propose using the 「Bread First Search」 algorithm to traverse the graph below and transform it into a tree structure. The starting point is the user's position.

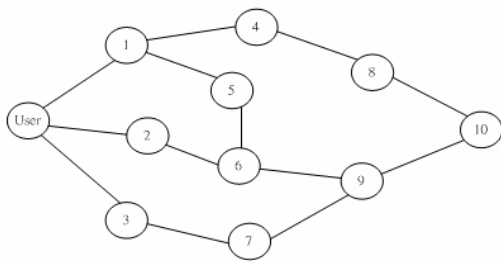


Figure 4: DMDB network

Figure 5 is the result after transforming the graph from the previous page into a tree structure. We then classify the media, and sequentially allocate the media into the physical network according to the defined order.

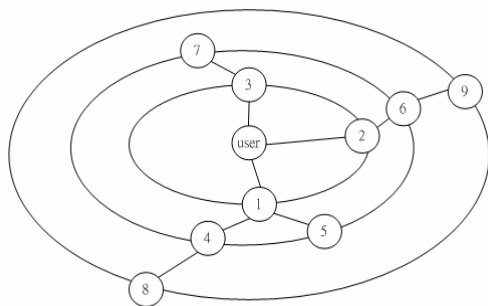


Figure 5: Tree structure of media

These are the basic steps used to determine potential paths through nodes. In the physical view we used link probability to model the network, multi-access to model the access probability, and moving patterns to improve the data allocation scheme.

#### 4. Logical View.

Logical View is concerned with learning sequence. The challenge is to use a course planning algorithm arranging a suitable learning sequence for a particular learner. In this section, we will apply the “minimum weight branching”[6] to solve course planning problems.

##### 4.1 The Learning sequence Environments.

Learning sequence environments introduces the concept of the learning environment and the concept of mapping real e-learning courseware unit to the

physical network topology, in other words from the logical view to the physical view. The reason for this is that, by doing so a network environment will provide better performance for learners to access course material. For example, Table 4 shows the entire contents of a math syllabus (calculus, linear algebra, discrete mathematics and so on). Each courseware unit has a capability indicator (Figure 2).

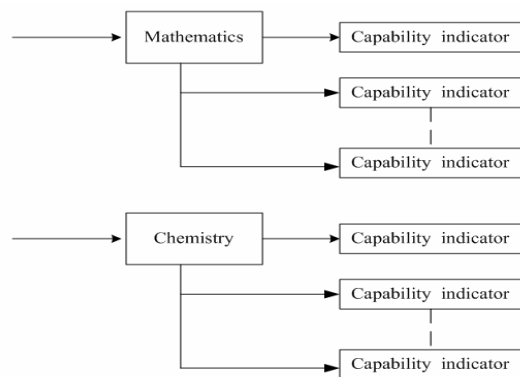


Figure 6: The Capability Indicator structure

Briefly, a capability indicator is used to describe a particular measurement (or capability factor a course provides) to the learner studying that a particular courseware unit and forms the basis for determining the capability for a learner to study another courseware unit. Each courseware unit can have several capability indicators (depicted in Figure 6).

Capability indicators are useful because they assist us with the management of the courseware unit, for example, the distribution of difficulty of each courseware unit and so on. Thus, in order to complete a curriculum, a learner has to obtain a certain number of capability indicators. We thus use capability indicators in our proposed model and apply it to the directed graph.

Table 4: A math program example

Node1 (course 1)	Calculus
Node2 (course 2)	Linear Algebra
Node3 (course 3)	Discrete Mathematics
Node4 (course 4)	Differential Equation
Node5 (course 5)	Probability Theory
Node6 (course 6)	Vector Analysis
Node7 (course 7)	Concrete Mathematics
Node8 (course 8)	Pattern Recognition

##### 4.2 Course Planning.

In the section 4.1, we briefly introduced an overview to the concept of capability indicator relations, the application of minimum weight

branching, dispatching them into the physical network environment.

In this section we explain, in detail, how to find a particular learning path (i.e. a sequence of courseware unit).

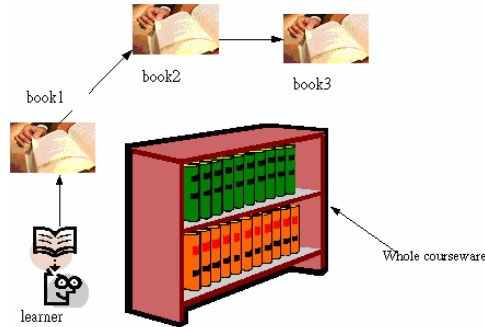


Figure 7: Idea of learning path

Suppose we have a book shelf (depicted in Figure 7) in the subject of mathematics. The book shelf can be depicted as an entire courseware unit selection in the curriculum. Each courseware unit (for example, algebra, geometry, discrete mathematics, vector analysis and so on) contains one or more capability indicators. The idea of learning paths is to find some books (courseware unit) that need to be studied in order to obtain all the capability indicators that are required. In the example depicted in figure 4, the learner needs to study book 1, book 2 and book 3 in order to obtain the required capability indicators and complete his curriculum. The purpose of this learning path is to save the learner's time by advising a proposed course plan.

We give an example here. Suppose we would like to find the least difficult path for a learner to completing a curriculum. In this example, we use eight nodes (courses). The root is at node eight and we would like to find the learning sequence path using minimum weight branching. Figure 5 shows the relationships between courseware units. Each node represents one course. The direction of arrows depicts the capability indicator relations with respect to one another. Each arrow is depicted by a difficulty level. In this example, our goal is to find learning sequence path for each node to node eight. Suppose a learner is currently at node 1, he has the choice of choosing either node 2, node 3 or node 4 as possible next stage course. This process continues until the learner reaches node 8 and all possible paths to node 8 are exhausted. In total, there are 8 possible paths with varying difficulties to completing the curriculum. To find the best sequence (i.e. the path with the least difficulty); we apply the minimum weight branching algorithm.

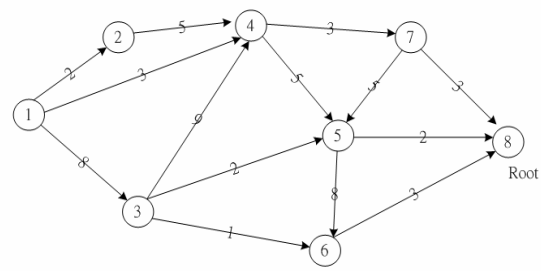


Figure 8: Relationship of courseware unit

Figure 8 depicts the initial relationships between each courseware unit. After applying the minimum weight branching algorithm to find the best learning path, we obtain our result, depicted in Figure 9.

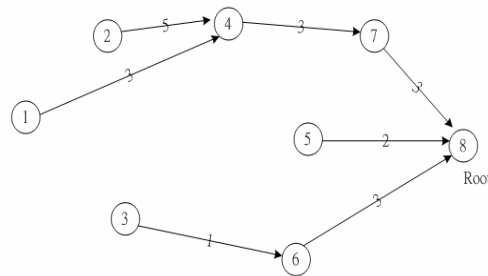


Figure 9: Branching of the relations

As a result, the best learning path for the learner at node 1 is node 1 -> node 4 -> node 7 -> node 8, and the difficulty is 9 (3+3+3)

Here we state all the learning paths and their difficulties.

- Learning path from node 1 is to take another 3 courses (in node 4, 7, 8), and the difficulty is 9(3+3+3).
- Learning path from node 2 is to take another 3 courses (in node 4, 7, 8), and the difficulty is 11(5+3+3).

The rest learning paths can be found as doing so by following the strategy we stated in the two steps we mentioned. We will not show all learning paths from all nodes to one another. Depending on where a learner is in the logical view, the minimum weight branching algorithm can be used effectively to find the best learning path to node 8.

## 5. Conclusion.

Here we summarize the issue we have mentioned before. In the Physical view, we use link probability and Multi-access Probability to formulate network reliability. In Logical view, we map the minimum weight branching to e-learning to suggest a learning sequence. Limitations for this research are

that statistic data and physical network parameters must be ready before these methods can be used to solve them.

## 6. References.

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