OLAP Query Processing via Subcubes

Kuo-Wei Ho De Lin Institute of Technology kwho@dlit.edu.tw Huei-Huang Chen Tatung University hhchen@ttu.edu.tw

Abstract-OLAP servers are increasingly being used by many organizations to provide multi-dimensional views which allow a better understanding of data for analysis purposes and provide better performance for analytical queries. Such OLAP queries are complex and time-consuming and hence materializing data cube is a commonly used technique to reduce response time. To our knowledge, most previous OLAP cube implementation techniques apply a static view selection algorithm on the search lattice. These static methods first treat each node in the lattice as an undividable unit and then pick some of them for materialization. Pre-computing some nodes without being aware of which nodes are actually accessed at run time would seriously impact both response time and available space. We propose to further partition nodes in the lattice into subcubes into each of which multiple OLAP queries via a dynamic materialization algorithm can be mapped. Experiments show that the locality effects do exist in OLAP queries, and our dynamic method keeps a reasonable performance even though the available space is very limited and is practical for OLAP query processing.

Keywords: data warehouse, OLAP, data cube, subcube.

1. Introduction

Data warehousing and On-line Analytical Processing (OLAP) technologies [4] have been one of the most important decision support systems in recent years. Inherently, OLAP queries are complex and time-consuming; hence materialization is a commonly used technique to reduce response time. To the best of our knowledge, applying view selection algorithms on the search lattice in advance is a common practice in most previous data cube implementation techniques. These static methods first treat each node in the lattice as an undividable unit and then pick some nodes for materialization. Furthermore, they depend heavily on some sampling techniques [11] to estimate the view size which is not practical in implementation.

Typically, generation of an OLAP cube can be accomplished by repeatedly computing group-bys based on the dimension levels, and the result forms a search lattice [12]. Note that the OLAP cube generated this way does not cover all aggregations it may have because a cube operation [8] can be further applied on the nodes in the lattice. Our experiments [6] on the APB-1 benchmark database show that the OLAP cube grew from 8 to 37 times as the size of the base fact table. The experimental result about growth ratio of the OLAP cube based on different implementations is shown in Figure 1.

The experimental result indicates that the density causes similar effects on both implementations even though the cube operation is not applied on each node in the lattice. Although currently we do not yet consider other factors that may impact the size of the OLAP cube including number of dimensions, cardinality and of levels of each dimension, we believe that density is intuitive and most representative factor in investigating the issues regarding the OLAP cube implementation and maintenance.

Not only few nodes in the lattice are accessed but a small portion within each accessed node is used. Therefore, careless materialized view selection strategies (or algorithms) may result in exhausting available system space with useless aggregations. Our experiments [6] also exhibit that only 13% nodes in the lattice are accessed in APB-1 Benchmark queries, and the accessed regions are much smaller than their corresponding nodes.

1.1. Proposed solution

With those issues mentioned above, we propose defining a finer but not too fine partition, subcube, for OLAP implementations. A finer partition contributes to more efficient space utilization than the whole node in the lattice. Experiments show that OLAP queries cluster only on some nodes in the lattice and hence it is critical that we select the right set to materialize. A partition that is not too fine allows potential locality effects, i.e. multiple OLAP queries can be mapped to the same subcube. Although part of subcube is sufficient to answer individual query, materializing the whole subcube introduce the possibility of reuse.

Instead of pre-computing some views for materialization, i.e. static method, without being aware of which views are actually accessed at run time, we also propose developing a dynamic view selection algorithm to materialize subcubes from existing ones. Generally, the algorithm materializes each accessed subcube as long as

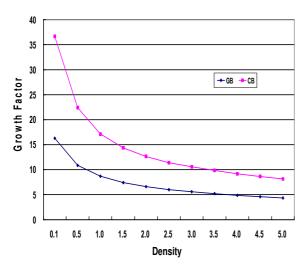


Figure 1. Growth ratio of different implementations

the available space is sufficient. While the space is exhausted, the algorithm should replace those subcubes with least reuse frequency based on certain replacement strategy.

1.2. Paper organization

The rest of the paper is organized as follows. In Section 2 we review current and past research activities related to the work presented here. Then in Section 3, we introduce the subcube framework to explain how to partition a node in the lattice into subcubes for materialization. We also illustrate how multiple queries can be mapped to the same subcube and the dynamic algorithm is provided to pick a set of subcubes for materialization. In Section 4 experimental results show that our subcube frame is almost immune to the change of density. Finally, we present our conclusions in Section 5.

2. Related Work

Previous studies related to OLAP implementations deal with two major problems at different levels. Research investigating the problem of how to compute an OLAP cube efficiently belongs to memory level, and has developed two major approaches including top-down and bottom-up [1, 15, 2, 3, 10], while those research on the problem of how to store an OLAP cube efficiently belongs to storage level, and has designed many algorithms to select the right set of view to materialize [12, 2, 7, 9, 14]. The most representative one is the greedy algorithm introduced in [12] choosing a near-optimal subset of views, while their heavy dependence on some sampling techniques [11] to estimate the view size which we think is not practical in implementation. In this paper, we propose a better partition for materialization and a new

technique for estimation of a view size. Through materializing subcubes, queries benefited from the results of previous are made possible.

3. The Subcube Framework

We can roughly view a subcube as the result of a drill-down operation to a cell (i.e. subcube cell) on each dimension it may have. There are two advantages in doing so. First the unit for materialization can be reduced from a node in a lattice to a finer partition – a subcube. Second the drill-down operation on each dimension will not result in a partition that is too fine as well as take potential locality effects into consideration. Before we illustrate the subcube framework, we introduce the *query cell notation* for representing OLAP queries concisely.

3.1. The query cell notation

We use the following example to demonstrate what information is specified in an OLAP query and how an answer to a query can be viewed as a result of drill-down operation to a cell.

Example 3.1 Consider the query description of *Channel Sales Analysis* (i.e. *Query 1*) defined in APB-1 benchmark queries [13]. For the sake of clarity, the query has been slightly modified to omit some details not directly relating to our discussion. This query shows *units sold* and *dollar sales* for *a given channel* by product, customer and time dimensions. The functional query definition is listed below.

get UNITS SOLD, DOLLAR SALES
by PRODUCT = children_of(prod)
by CUSTOMER = children_of(cust)
by TIME = children_of(time)
where CHANNEL = chan

Note that the member_name in parentheses is a parameter denoting a data member regarding a certain dimension, and *children_of(x)* denotes its children data members of x. The above query can be represented as a 4-tuple (*prod, cust, chan, time*) in our notation. The underlined elements are group-by attributes used to specify along which dimensions the measures are analyzed in the query. The element not underlined is slicer attribute used to restrict which data member of a certain dimension is extracted. We assume that all measures are analyzed in each query, so there is no need for us to specify measures in our query notation.

For an n-dimensional data cube, a query cell is an *n*-tuple representing an OLAP query. Each slicer attribute contributes to a constituent element of the n-tuple, and those dimensions involved in group-bys are marked by underlines in corresponding slicer attribute.

Since the *chan* is identified as a slicer attribute, and *prod*, *cust* and *time* are involved in group-by clauses, then

according to our notation the above query will be represented as the query cell (*prod, cust, chan, time*).

Simply put, our goal is to keep query representation simple for discussion as well as be used to dynamically identify the *correlation* among multiple queries which would be beneficial in materialization. Our practice is to define a *subcube* based on multiple correlated queries (in query cell notation) as an undividable unit for materialization. Owing to the fact that one materialized subcube could be reused by multiple queries for multiple times, the total query cost will be effectively reduced. We describe the process of query cell mapping in the following subsection.

3.2. Mapping of query cells

Though we represent an OLAP query as a query cell, how can we obtain some useful clues for materialization from queries? Our practice is to moderately *enlarge* the queried aggregations to one of more *subcubes*. That is to say we define the subcube as an undividable unit for materialization and users' queries are transformed into queries on one or more subcubes. Although we may have materialized some aggregations not yet be used, we do take the potential of *locality* effects into consideration.

Strictly speaking a query cell may access a portion of a certain subcube or multiple subcubes (if range value is used). Through materializing the whole subcube(s) it raises the possibility of reuse since multiple query cells may queried to the same subcube(s). Owing to the fact subcubes are further partitions of a node in the lattice, intrinsically subcubes can be classified according to the node it belongs to, namely subcube class represented by scClass_(m,n,o,p) for a 4-dimensional data cube. The subscripts denote the corresponding dimension levels (the formal definition is postponed in the next subsection) and the larger the value is the more detailed is the subcube class. Take APB-1 Benchmark database for example, the number of levels of Product, Channel, Customer and Time dimensions are 7, 3, 2 and 3, respectively. And we also adopt product, channel, customer and time as the dimension order in describing the subcube classes. Then scClass_(7,3,2,3) means the most detailed node in which data members belong to Code, Store, Base and Month levels, respectively. Similarly, scClass_(4,2,1,2) denotes constituent member of the cells within it belong to Family, Retailer, Top and Quarter levels, respectively. The complete relation schemas of APB-1 Benchmark database are listed below (the subscripts denote corresponding dimension level numbers).

SalesFact(Code, Store, Base, Month, UnitsSold, DollarSales) ProdDim(Code7, Class6, Group5, Family4, Line3,

Division₂, Top₁) ChanDim(Store₃, Retailer₂, Top₁)

CustDim(Base₂, Top₁) TimeDim(Month₃, Quarter₂, Year₁)

Subcubes are finer partitions of a node in the lattice, therefore we need to devise a notation similar to the way we represent queries to define subcubes. The representation we adopted here is called *subcube cell* similar to the query cell is an *n*-tupple except each constituent element has a superscript and jointly representing the ultimate subcube class it belongs to. Generally, accepting a query cell it is then mapped, by the the *CellMapping* procedure (defined in following subsection), into a subcube cell to define a subcube. Due to the fact that the same n-tuple can be used to define multiple subcubes in various subcube classes, to avoid ambiguity it is necessary to retain the superscripts in the query cell. We take following example to illustrate how multiple query cells would query to the same subcube.

Example 3.2 Consider that there are two dimensions sales fact is analyzed. Two queries (*Taipei2*, 200301₃) and (*Breeze*₃, <u>2003Q1</u>₂) are issued consecutively (the subscripts used here denote corresponding level numbers). According to the *query cell notation*, both cells *drill-down* to the most detailed aggregations, i.e. $scClass_{(Store, month)}$, by *CellMapping* procedure; besides, with the *parent-child* relationships exist: *Taipei2-Breeze*₃ and 2003Q1₂-200301₃, then both cells will be mapped to the same subcube cell (*Taipei*, 2003Q1). In other words, the subcube $sc(Taipei^3, 2003Q1^3)$ is referenced by both query cells. The formal definitions of *CellMapping* procedure is explained in following subsection.

3.3. The subcube

Although the terms "data cube" and "OLAP cube" are commonly used and even interchangeable in the literature investigating multidimensional databases or OLAP systems, we take a different view. Basically, we regard the data cube as the result of a cube operation [8], while the OLAP cube is the union of applying cube operation on each node in a cube lattice [12].

Definition 3.1 [The Data Cube] A *data cube* is the result set of the **cube operator**. For an n-dimensional data cube, the **cell** is an (n+m)-tuple in the form of $(d_1, d_2, ..., d_n, f_1(x_1), f_2(x_2), ..., f_m(x_m))$, where

- Each d_i is either a value from the domain of dimension levels of the *i*-th **Dimension** or an **ALL** values;
- Each $f_j(x_j)$ is a value generated by the aggregate function defined on the data cube.

If the cardinality of the *n* attributes are $C_1, C_2, ..., C_n$, then the number of cells of the *n*-dimensional data cube is at most $\prod_{i=1}^{n} (C_i+1)$, and the number of super-aggregates (*i.e. those cells containing ALLs*) is $\prod_{i=1}^{n} (C_i + 1) - \prod_{i=1}^{n} C_i$.

In real-life applications, hierarchies exist in dimensions and underlie two important querying operations: drill-down and roll-up. Based on the dependency relation \leq [12], each *GB* form a cube lattice.

Definition 3.2 [The Cube Lattice] Given n dimensions D_1 , D_2 ,..., D_n and each with a set of dimension levels (hierarchy)

$$\begin{split} L_{1} &= \left\{ l_{1}^{1}, l_{1}^{2}, ..., l_{n}^{h_{1}} \right\}, \\ L_{2} &= \left\{ l_{2}^{1}, l_{2}^{2}, ..., l_{2}^{h_{2}} \right\}, \\ ... \\ L_{n} &= \left\{ l_{n}^{1}, l_{n}^{2}, ..., l_{n}^{h_{n}} \right\} \ respectively \end{split}$$

Then the set $L = \{L_1 \times L_2 \times ... \times L_n\}$ and dependence relation \leq forms a Cube Lattice $\langle L, \leq \rangle$ with $|L_1| * |L_2| * ... * |L_n|$ nodes.

Definition 3.3 [The Node Operations] Given an n-dimensional fact f and the corresponding cube lattice $\langle L, \leq \rangle$, for each element $(l_1, l_2, ..., l_n) \in L$, the set of its constituent elements $\{l_1, l_2, ..., l_n\}$ can be used to compute group-by and cube operations from f denoted by $GB(l_1, l_2, ..., l_n)$ and $CB(l_1, l_2, ..., l_n)$.

Each node of an n-dimensional cube lattice is an n-tuple, and its constituent elements can be used as group-by attributes to generate the node value. The computation is first joining the fact table with each dimension tables then grouping it by its constituent elements.

Definition 3.4 [The Node Value] Given an n-dimensional cube lattice $\langle L, \leq \rangle$, for each element $(l_1, l_2, ..., l_n) \in L$, the corresponding node in the lattice is denoted by $Node_{(l_1,l_2,...,l_n)}$ or $scClass_{(l_1,l_2,...,l_n)}$, and its value is the result of cube operation applying on it.

Since each node of the cube lattice is further partitioned into subcubes, to better express the concepts regarding the subcube, a node in the lattice is usually referred to as a subcube class represented by scClass in our discussion.

Definition 3.5 [The OLAP Cube] Given an *n*-dimensional cube lattice $\langle L, \leq \rangle$ with **q** nodes, the **OLAP cube** is the **union** of q data cubes.

 $CB_{OLAP}(L) = \{ CB(s_1) \cup CB(s_2) \cup \dots \cup CB(s_a) \mid \forall s_i \in L \}$

Generally, an OLAP query is a subset of a subcube. To be benefited from potential locality effects, not only the

result of an OLAP query is materialized but the entire subcube. We demonstrate how a query cell is mapped into a subcube, and how a materialized subcube can be used to answer multiple queries in following example. Before we formally define the subcube, some useful functions are listed below.

- *level(x):* returns the level name of *x*.
- *child_level(x)*: returns the child level name of *x*.
- parent(x): returns the parent name of x.

Definition 3.6 [The Subcubes] Given an CB_{OLAP}(L) and a query cell $(c_1, c_2,..., c_n)$, the corresponding **subcube** is represented by $sc\left(s_1^{l_1}, s_2^{l_2}, ..., s_n^{l_n}\right)$, where

•
$$s_i = \begin{cases} c_i \text{ if } c_i \text{ is underlined} \\ parent(c_i) \text{ if } x \text{ not underlined} \end{cases}$$

• $l_i = \begin{cases} child _level(c_i) \text{ if } c_i \text{ is underlined;} \\ level(c_i) \text{ if } c_i \text{ not underlined.} \end{cases}$

and its values is a subset of a data cube $CB(l_1, l_2, ..., l_n)$, where each cell share the same parent-child relationship.

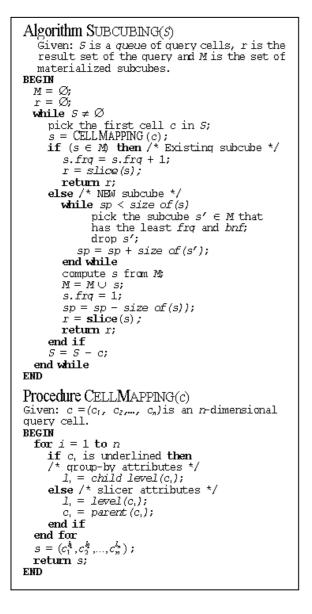
$$sc(s_1^{l_1}, s_2^{l_2}, ..., s_n^{l_n}) = \{(c_1', c_2', ..., c_n', a_1, a_2, ..., a_m) | c_i' = parent(s_i), \forall i = 1, 2, ..., n\}$$

3.4. The SUBCUBING Algorithm

We develop a dynamic algorithm SUBCUBING based on our subcube framework. Generally, Algorithm SUBCUBING materializes each accessed subcube as long as the space is available. If the remaining space is not sufficient, the algorithm repeatedly replaces the old subcube that has the least reuse frequency until space become sufficient again to materialize a newly accessed subcube. There are some variables used in the algorithm to facilitate the materialization processing: The variable sp denotes the size of available space allocated and it shrinks with time. To determine the least recently used subcube, we use the variable frq to keep track of the reuse frequency for each materialized subcube. In addition, the variable *bnf* is used to denote the potential benefit it may has. The unit for materialization in the algorithm is individual subcube, and it always keeps the most frequently used subcubes in storage as long as the remaining available space is sufficient.

4. Experimental Results

We have implemented the dynamic algorithm we developed and the greedy algorithm developed in [12] for comparison. The system used is a Pentium 4 2.8G Hz with 2GB DDR 400 SDRAM, running Microsoft Windows Server 2003 and SQL Server 2005. The algorithm was



implemented using Microsoft Visual Basic 6.0 and ActiveX Data Model (ADO). We also implemented the greedy algorithm [12] for comparison.

4.1. The sample data

The sample data used in our experiments is produced by APB-1 OLAP Benchmark Release II File Generator. The common parameters used in these experiments are: channel = 10, number of users = 100 (for enough query streams). Besides, the densities are 0.1, 1.0 and 5.0, respectively. To exactly compute the size of each subcube class, we materialize complete subcube classes in advance instead of using some sampling techniques [11]. Then we analyze the queries mixed of 4 types (only these queries are considered directly related to our Sales cube).

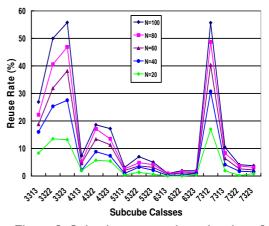


Figure 2. Subcube reuse ratio at density = 0.1

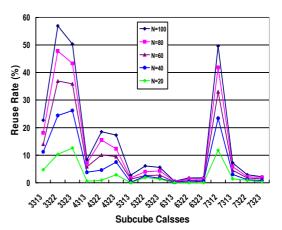


Figure 3. Subcube reuse ratio at density = 1.0

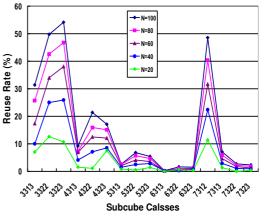


Figure 4. Subcube reuse ratio at density = 5.0

4.2. Results

Experimental results show that our method partitioning subcube classes into subcubes is almost immune from

density. The subcube reuse ratios in individual subcube classes at different density are shown below in Figure 2, Figure 3 and Figure 4.

We compare the hit rates with the static method, i.e. Greedy Algorithm in [5]. The results show that pre-computing some views without being aware of the actual usage at run time performs poorly. Note that with the additional space larger than 1.5 times as large as the size of base fact the hit rate no longer increase. According to our experiments, the dynamic algorithm we developed can rapidly determine the right set of *subcube* to materialize without consuming excess additional space. While the static Greedy algorithm [9] needs 4 times additional space selecting 33 *subcube classes* to cover the most reused top 5: $scClass_{(3,3,1,3)}$, $scClass_{(3,3,2,3)}$, $scClass_{(3,3,2,3)}$, $scClass_{(3,3,2,3)}$.

5. Conclusion and Future Work

We have investigated the problem of further partitioning the subcube class into subcubes in order to raise its reusability. We experimented on the APB-1 Benchmark database and emphasized the need to handle the serious situation that most OLAP queries focus only on certain subcube classes and sometimes even a small portion within a subcube class. We also developed one dynamic view selection algorithm to rapidly determine frequently used subcubes. Through moderately enlarge the size of aggregations queried to subcube(s) potential locality effects are taken into consideration, and at the same time reusability is made possible. We believe that the subcube framework will also apply to other OLAP data models.

References

- [1] S. Agrawal, R. Agrawal, P.M. Deshpande, J.F. Naughton, R. Ramakrishnan, and S. Sarawagi. "On the Computation of Multidimensional Aggregates," *Proc. of 22th International Conference on Very Large Data Bases(VLDB 1996)*, pp. 506-521.
- [2] E. Baralis, S. Paraboschi, and E. Teniente, "Materialized View Selection in a Multidimensional Database," *Proc. of 23th International Conference on Very Large Data Bases (VLDB 1997)*, pp. 156-165.
- [3] K.S. Beyer and R. Ramakrishnan, "Bottom-up Computation of Sparse and Iceberg Cubes," Proc. of ACM SIGMOD International Conference on Management of Data (SIGMOD 1999), pp. 359-370.

- [4] S. Chaudhuri and U. Dayal, "An Overview of Data Warehousing and OLAP Technology," *SIGMOD Record*, Vol. 26, No. 1, pp. 65-74.
- [5] H.-H. Chen, K.-W. Ho, and C.-L. Shiou, "An Implementation for Subcube-based Query Processing," *Proc. of International Computer Symposium (ICS 2004).*
- [6] H.-H. Chen and K.-W. Ho, "Implementation Data Cubes via Subcubes," *Proc. of the International Database Engineering and Applications Symposium* (*IDEAS 2004*), pp. 378-386.
- [7] H. Gupta, "Selection of Views to Materialize in a Data Warehouse," *Proc. of International Conference on Database Theory (ICDT 1997)*, pp. 98-112.
- [8] J. Gray, A. Bosworth, A. Layman, and H. Pirahesh, "Data Cube: A Relational Aggregation Operator Generalizing Group By, Cross-Tab, and Sub-Totals," *Proc. of the 12th International Conference on Data Engineering (ICDE 1996)*, pp. 152-159.
- [9] H. Gupta, V. Harinaryan, A. Rajaraman, and J.D. Ullman, "Index Selection for OLAP," *Proc. of the* 12th International Conference on Data Engineering (ICDE 1997), pp. 208-218.
- [10] J. Han, J. Pei, G. Dong, and K. Wang, "Efficient Computation of Iceberg Cubes with Complex Measures," *Proc. of ACM SIGMOD International Conference on Management of Data (SIGMOD 2001)*, pp. 1-12.
- [11] P.J. Haas, J.F. Naughton, S. Seshadri, L. Stokes, "Sampling-Based Estimation of the Number of Distinct Values of an Attribute," *Proc. of 21th International Conference on Very Large Data Bases* (VLDB 1995), pp. 311-320.
- [12] V. Harinarayam, A. Rajaraman, and J.D. Ullman, "Implementing Data Cubes Efficiently," Proc. of ACM SIGMOD International Conference on Management of Data (SIGMOD 1996), pp. 205-216.
- [13] OLAP Council, "OLAP Council APB-1 Benchmark Specification," White Paper, 1998.
- [14] A. Shukla, P.M. Deshpande, and J.F. Naughton, "Materialized View Selection for Multidimensional Datasets," *Proc. of 24th International Conference on Very Large Data Bases (VLDB 1998)*, pp. 488-499.
- [15] Y. Zhao, P. Deshpande, J. F. Naughton, "An Array-based Algorithm for Simultaneous Multidimensional Aggregates," Proc. of ACM SIGMOD International Conference on Management of Data (SIGMOD 1997), pp. 159-170.