

A Simple File Assignment Method to Maximize the System Reliability in Distributed Computing Systems under Memory Space Constraints

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Abstract

Distributed computing systems (DCS) have become a major trend in today's computer system design due to their capability for offering high speed and high reliable performance advantages. Reliability is an important issue in DCS design for military application. The distribution of programs and data files are two important factors that affect the program reliability and system reliability. The reliability-oriented file assignment problem is to find a file distribution such that the program reliability or system reliability is maximal. In this paper, we develop a simple heuristic file assignment algorithm which use several simple heuristic assignment rules to achieve reliability-oriented file assignment. The proposed algorithm can obtain the optimal solutions in most cases and reduce computation time significantly.

1. Introduction

A distributed computing system is a collection of processor-memory pairs connected by a communication subnet and logically integrated by a distributed operating system and/or a distributed database system [1,2,3]. Potential advantages of a DCS are significant, including good performance, reliability, resource sharing, and extendibility. Performance enhancement is due to the use of multiple processors and efficient subnets. Reliability improvement is due to the use of redundant techniques in data files, programs, processes, and communication devices. A program in a DCS may require one or more data files located in different computers for execution. The distribution of data files can affect program reliability and overall system reliability. An important problem in DCS design is to find a file distribution such that a certain reliability measure is maximal. Several network reliability measures have been defined and associated evaluation methods have been developed. The concepts of distributed program reliability (DPR) and distributed

system reliability (DSR) in [4,5] and the reliability evaluation algorithm in [13,14] are adopted in this paper.

The file assignment problem and related programs such as task assignment and job scheduling have been studied for many years [6,7,8,9]. Since the file assignment problem is NP-complete [10], Wang [11] proposed a reliability-oriented file assignment algorithm to solve the optimal file assignment problem under a memory space constraint. This method is capable of finding the optimal solution, but it is not efficiently. Hwang & Tseng proposed a heuristic task assignment algorithm for the k-DTA problem to maximize reliability of a distributed system under some resource constraints [12]. The k-DTA algorithm assigns fixed number of copies of programs and data files only, so the system utilization is not maximized. In addition, the algorithm is quite complex. This paper presents a simple but effective heuristic algorithm for reliability-oriented file assignment problem. The Simple File Assignment algorithm use a special Minimum Selection Rule and Grouping Rule based upon some heuristics [11,12] to find a file distribution such that the DPR (or DSR) is maximal and the memory limitation constraint of each processing element is satisfied. Numerical results are given through computer simulation to show the solution of our proposed algorithms.

2. Notation, Definitions, and Problem statements

Notation & Acronyms:

| | |
|----------|--|
| $G(V,E)$ | An undirected graph; V, E: set of [vertices, edges/links] in the graph |
| N_i | node i in V |
| L_{ij} | link between N_i and N_j |
| PRG | the set of programs allocated in the network for execution |
| F_s | the set of files required by PRG |
| PRG_p | program p in PRG |
| F_i | file i in F_s |

| | |
|----------------------|---|
| n | number of nodes in G; $n = V $ |
| k | number of files in F_s |
| l | number of programs in PRG |
| p(q) | probability that the communication link works (fails) |
| PA _i | The set of programs allocated on N _i |
| FA _i | The set of files allocated on N _i |
| E(PRG _p) | event that PRG _p can successfully run and files can be successfully accessed by PRG _p |
| Pr(E) | probability of event E |
| ROFA | Reliability-Oriented File Assignment |
| SFA | Simple File Assignment algorithm |

Definitions:

- FST: a file spanning tree that connects the root node (the processing element that runs the program under consideration) to some other nodes such that its vertices hold all the needed files.
- MFST: a minimal FST such that there exists no other FST which is subset of it.
- DPR: The probability that a given program can be run successfully and will be able to access all the files it requires from remote sites in spite of faults occurring among the processing elements and communication links. The MFSTs connect the root node (the PE that runs the program under consideration) to other nodes such that these nodes hold all the files needed for the program under execution. The DPR and DSR can then be determined by computing the probability that at least one of these MFSTs is working. Thus the distributed program reliability for a given program j can be defined as the probability that at least one MFST of a given program j is operational [4,5]. This can be written as

$$DPR = \Pr \left(\bigcup_{j=1}^{n_{mfst}} MFST_j \right)$$

where n_{mfst} is the number of MFSTs that run the given program.

- DSR: The probability that all the programs in the system can be run successfully. The DPR measures the reliability of a particular distributed program. For the entire DCS to be operational, several such programs or a given set of distributed programs must be operational. A system level reliability measure for l distributed programs to be operational is defined in [15] as

$$DSR = \Pr \left(\bigcap_{i=1}^l PRG_i \right)$$

- MFFC: An MFFC is a maximal feasible file combination such that there exists no other feasible file combination which is a superset of it. If a combination $X_i^{(t)} = (x_{i1}^{(t)}, x_{i2}^{(t)}, \dots, x_{ik}^{(t)})$ is said to be a feasible file

combination of node N_i, then

$$\sum_{j=1}^k s_j x_{ij} \leq C_i$$

where C_i = the available memory space of node i (N_i)

s_j = size of file j (F_j)

x_{ij} = the indicator of file assignment; x_{ij} = 1 if F_j is assigned to N_i, otherwise x_{ij} = 0

- Node Environment Weight Heuristics: Node X₁ is more reliable than node X₂ if and only if the degree of X₁ is higher than that of X₂ [12]. It is because the node with higher degree is more likely to have more paths to the destination nodes than those with lower degrees. The node environment weight represents the composite reliability for the nodes and links surrounding a node.

$$ENV_WEIGHT(N_i) =$$

$$R(N_i) \cdot \sum_{N_j \in ADJ(N_i)} R(N_j) \cdot R(L_{ij})$$

where ADJ(N_i) = set of nodes which are adjacent to N_i

R(N_j) = Pr{N_j is operational}

R(L_{ij}) = Pr{L_{ij} is operational}

- Program Weakness Heuristics: Program P₁ is weaker than program P₂ if and only if the minimum number of nodes required to assign P₁ and its associated files are greater than those required for P₂ [12]. We simply use the total memory of P₁ and its associated files to approximate the number of nodes required. The weakness decision function is:

$$WEAKNESS(P_i) = SIZE(P_i) + \sum_{F_j \in FN_i} SIZE(F_j)$$

Problem statements:

The reliability-oriented file assignment problem can be mathematically stated as follows:

Problem - Maximizing DSR subject to memory space constraint

$$\text{Maximize DSR} = \Pr \left[\bigcap_{i=1}^l E(PRG_i) \right], \text{ subject to}$$

$$\sum_{j=1}^l SIZE(P)_j X_{ij} + \sum_{j=1}^k SIZE(F_j) Y_{ij} \leq C_i, \forall$$

$$N_i, i = 1, 2, \dots, n$$

$$\sum_{i=1}^n X_{ij} \geq 1 \quad j = 1, 2, \dots, l$$

$$\sum_{i=1}^n Y_{ij} \geq 1 \quad j = 1, 2, \dots, k$$

X_{ij} = 1 if P_j is allocated on N_i, otherwise X_{ij} = 0

Y_{ij} = 1 if F_j is allocated on N_i, otherwise Y_{ij} = 0

For the reliability-oriented file assignment problem, we give:

- a) network topology

- b) files required by each program for execution
 - c) the size of each program and data-file
 - d) the available memory space of each processing element (computer node)
 - e) the reliability of each node and communication link
- This paper is concerned with the file assignment to maximize the system reliability of the distributed computing system under memory space constraints.

3. The Simple File Assignment algorithm

This section presents a Simple File Assignment (SFA) algorithm which use the MFFC concept, program weakness and node environment weight heuristic measures. We also simplify the assignment method by introducing two new concepts called the Minimum Selection Rule and Grouping Rule. The combined effort makes our new algorithm simple and efficient.

3.1 Minimum Selection Rule (MSR)

From the definition of the MFFC, we know that the MFFCs give us the best reliability for each node. For a file assignment problem with size of each program and files given, there are several MFFC combinations for a single node with limited storage capacity. The basic idea for the SFA algorithm is using MSR to pick up just one or two good MFFCs for each node. The MSR algorithm is simple with reducing computation time very much. This heuristic reduction makes original intractable problems solvable and the reliability deviation from the optimal solution is also tolerable by simulation results.

Example 1: Suppose we know that programs P_1, P_2 need file $\{F_1, F_2\}$ and $\{F_1, F_3\}$ to execute successfully. The size of node N_1 is 3 and the sizes of program P_1, P_2 and file F_1, F_2, F_3 are 1, 2, 1, 2 and 3, respectively (i.e., $SIZE(P_i) = i$ and $SIZE(F_i) = i$). We can compute all the MFFCs for node N_1 and show the result in table 1.

Table 1: All the MFFCs for node N_1 of Example 1

| Node N_1 (MFFCs) | P_1 | P_2 |
|----------------------|-----------------------|-----------------------|
| $a_1 = \{P_1, P_2\}$ | $F_1 + F_2 = 3$ | $F_1 + F_3 = 4$ |
| $b_1 = \{P_1, F_1\}$ | $F_2 = 2$ | $P_2 + F_3 = 5$ |
| $c_1 = \{P_2, F_1\}$ | $P_1 + F_2 = 3$ | $F_3 = 3$ |
| $d_1 = \{P_1, F_2\}$ | $F_1 = 1$ | $P_2 + F_1 + F_3 = 6$ |
| $e_1 = \{F_1, F_2\}$ | $P_1 = 1$ | $P_2 + F_3 = 5$ |
| $f_1 = \{F_3\}$ | $P_1 + F_1 + F_2 = 4$ | $P_2 + F_1 = 3$ |

Assume we wish to favor program P_1 for node N_1 (it is decided by program weakness and node environment weight heuristics), we sum up the sizes of all the lacking components of set $\{P_1, F_1, F_2\}$ for each MFFC. We do this because $\{P_1, F_1, F_2\}$ is the set of complete requirement for

successful execution of program P_1 . If we assign MFFC $a_1 = \{P_1, P_2\}$ to this DCS, the other nodes of this DCS must supply the remaining F_1 and F_2 for P_1 to run successfully. It goes without saying that $d_1 = \{P_1, F_2\}$ is more favorable than $a_1 = \{P_1, P_2\}$ for P_1 because d_1 is more self-sufficient (i.e., d_1 lacks F_1 only, while a_1 lacks both F_1 and F_2).

From table 1, we can see (in bold & italic face) MFFC $d_1 = \{P_1, F_2\}$ and $e_1 = \{F_1, F_2\}$ are indistinguishable to Minimum Selection Rule because the weight of their lacking component is identical. However, MSR has successfully reduced the number of possible MFFCs of node N_1 from 6 to 2, a three-fold speed up just for a single node N_1 . The combined effort of MSR for every node is very significant.

3.2 Grouping Rule (GR)

Before we go into the details about the Grouping Rule, let's observe some optimal file assignment cases.

Example 2: In Figure 1, the optimal solutions are the sets whose union of node N_2 's MFFC and node N_3 's MFFC is the full set $\{P_1, P_2, F_1, F_2, F_3\}$ of the DCS. The node N_1 's MFFC is irrelevant, however.

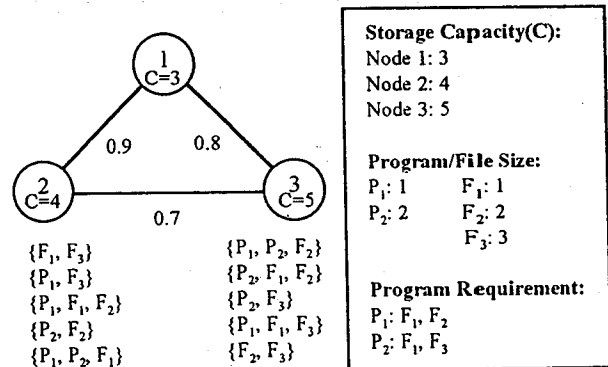


Figure 1. The optimal file assignments of Example 2

The definition of the Full Set is: a set which contains all the programs and their required data files in the DCS. Node 2 and node 3 in the example 2 obviously contain a single full set $\{P_1, P_2, F_1, F_2, F_3\}$. Full set is the basic requirement of the DSR. Let's recall the definition of the minimum file spanning tree. The MFST for all programs must contain all the elements in the full set. If not, at least one of the programs will fail so the DSR value is zero. In addition, denote the set of MFSTs for an assignment $ASS(S, G)$ of a dependent set by $MFST(S, G)$. If there exists another assignment $ASS(S - \{v\}, G)$ where v is a terminal node of some MFST in $MFST(S, G)$, then $DSR(S, G) < DSR(S - \{v\}, G)$. This theorem is obvious from the definition of DSR.

Let's examine the result of example 2. The optimal assignment is the spanning of all programs and their files

on the node 2 and node 3 in the full set. From previous theorem we know this assignment is better than other assignments which full set must span all the three nodes. But how do we make a choice between two or more file assignments with the same maximum number of full sets? Figure 2 is an optimal file assignment to this DCS and Figure 3 is a poor one. They differ only in the file assignments. This DCS has several groups of nodes which contain the full set $\{P_1, P_2, P_3, F_1, F_2, F_3, F_4\}$.

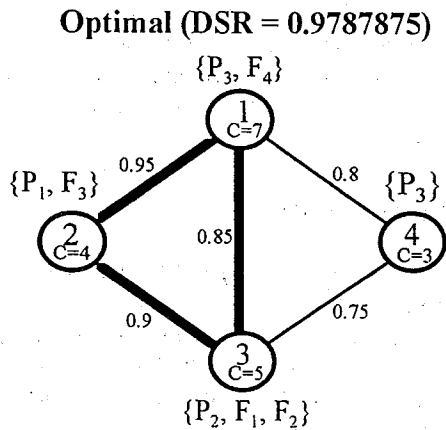


Figure 2. The optimal file assignment of Example 4

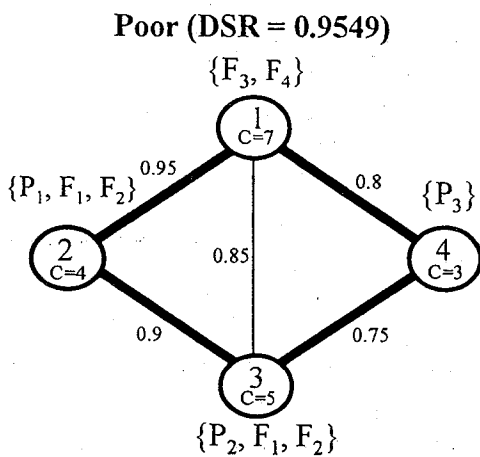


Figure 3. The poor file assignment of Example 4

Figure 2 and 3 is an example to show how file assignments affect the distributed system reliability. First we know that the file assignment which contains more groups of nodes with full set is more reliable. To prove this theorem, let's recall how distributed system reliability is computed. The DSR is the probability of the union of the number of MFSTs that run the given program. The MFST spans one of the full sets we just discovered. If there are more full sets in the DCS, the number of MFSTs is also larger, hence the DSR should be greater because of $P(A \cup B) \geq P(A)$ by the set theory. These are some hints

we got from the previous observations: a) A file assignment which has greatest number of groups with full set is our preferred choice, and b) If there are two or more file assignments which contains the same number of groups with full set, the one which groups with full set reside on less number of nodes and their center on stronger nodes is our preferred choice. For each heuristic guess, we will select the best one by following criteria:

- The number of full set is maximum.
- These full sets occupy minimum number of nodes.
- These full sets which have stronger nodes.

The Grouping Rule provides good estimates to those MSR selections and gives us a quite precise method to pick up near-optimum file assignments.

3.3 The Simple_File_Assignment algorithm

The Simple File Assignment algorithm consists of five steps:

Step1: Initialization

Step2: Determine the MFFCs for each node

We try every possible combinations of program and file distributions, check this combination's storage capacity and compare it with all MFFCs in the 'found' list. If the new found MFFC is over-sized, ignore it. If it is a superset of previously found MFFCs, delete those MFFCs in the 'found' list.

Step3: Determine the program weakness and node environment weight measures

For program weakness, we add the size of program and all its needed files and does a sort to determine the order. For environment weight, we just add all the link reliabilities for each node under the simplifying assumption of perfect node and does a sort to determine the order.

Step4: Use Minimum Selection Rule to choose good MFFCs

We generate the heuristic Minimum Selection Table and assign weak program to strong node.

Step5: Use Grouping Rule to determine the near-optimum file assignment

We check all our file assignments in Step 4 and pick up the one which has maximum number of full sets. If there are two or more assignments which have maximum number of full sets, we check if the new one occupy less nodes. If two or more assignments occupy the same number of nodes, we check which assignments own stronger nodes.

3.4 The Complete SFA algorithm

Algorithm Simple_File_Assignment;

```

begin
  Step1: Initialization
  Step2: Determine the MFFCs for each node
    for n = 1 to Number_of_Nodes do
      MFFC[n,i] = 0 /* clear i'th MFFC for Node n */
      NC = 0 /* Node Capacity */
      for i = 2(F+P) downto 1 do /* i is a FFC's bit
        representation */
          add File/Program Size to NC
        if NC < (This Node's Maximum Capacity) then
          MFFC[n,nm] = FFC /* add this FFC to the
            list of MFFCs */
          for k = 1 to nm do /* nm: the number of the
            list of MFFCs */
            if FFC is a superset of MFFC[n,k] delete
              MFFC[n,k]
        Step3: Determine the program weakness and node
          environment weight measures
          for i = 1 to Number_of_Programs do
            for j = 1 to Number_of_Files do
              if (program i needs file j) then weak[i] = weak[i]
                + FileSize[j]
            sort the weak[i] array
          for i = 1 to Number_of_Nodes do
            for j = 1 to Number_of_Edges do
              if (node i has edge j) then weight[i] = weight[i]
                + Link_Rel[j]
            sort the weight[i] array
        Step4: Use Minimum Selection Rule to choose good
          MFFCs
          for i = 1 to Number_of_Nodes do
            for j = 1 to Number_of_Programs do
              for k = 1 to Number_of_MFFCs[i] do
                m = (program j and files needed) - MFFC[i,j]
                /* m: remaining prg/file*/
                if m < min_m then m = min_m /* pick up
                  the minimum */
              for i = 1 to Number_of_Nodes do
                do the assignment (one-by-one)
            Step5: Use Grouping Rule to determine the near-
              optimum file assignment
            for cnt = 1 to Number_of_Minimum_Selections do
              for i = 1 TO 2Number_of_Nodes do /* i : Set of Nodes
                bit representation */
                if (set i = FullSet) then FS = FS + 1 /* i :
                  Number of FullSets */
                if FS > MaxFS then MaxFS = FS /* i : find the
                  maximum # of FullSets */
                if FS = MaxFS then Check_Stronger_Nodes
            end
  end
  
```

3.5 Time complexity analysis

The time complexity of the SFA algorithm is analyzed and summarized in table 2.

Table 2: The time complexities for SFA algorithm

| Step | Complexity |
|-------|---|
| 1 | $O(1)$ |
| 2 | $O(n \cdot 2^{p+f})$ |
| 3 | $O(p \cdot f) + O(p \log p) + O(n \cdot e) + O(n \log n)$ |
| 4 | $O(n \cdot p \cdot m) + O(n)$ |
| 5 | $O(s \cdot 2^n)$ |
| Total | $O(n \cdot 2^{p+f} + n \log n + n \cdot p \cdot m + s \cdot 2^n)$ |

where (n, p, f) = number of (nodes, programs, files),
e = number of edges of the node,
m = number of MFFCs of the node,
s = number of minimum selections.

From table 2, we therefore conclude that the complexity of SFA algorithm is bound by step 2 or step 5.

4. Illustrative examples & Simulation results

Example 3: For a simple distributed computing system with parameters is shown in Figure 4, we apply our Simple File Assignment algorithm to it to show how it works.

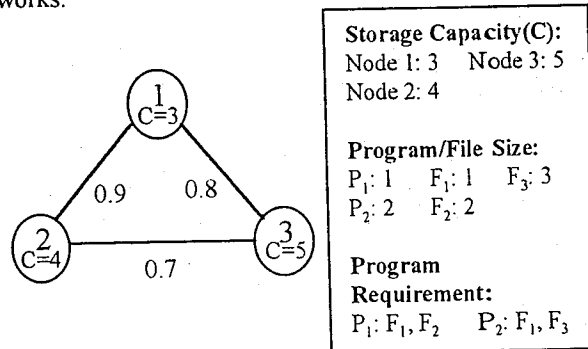


Figure 4. Network topology and data requirement of Example 3.

First, We try every possible combinations of program and file distributions to determine the MFFCs for each node. The left column of table 3 lists all the MFFCs of each node. Then, we compute the program weakness and the node environment weight. The program weakness measure is the sum of the size of the program itself and all required files for successful execution, so $WEAKNESS(P_1) = SIZE(P_1) + SIZE(F_1) + SIZE(F_2) = 1 + 1 + 2 = 4$ and $WEAKNESS(P_2) = SIZE(P_2) + SIZE(F_1) + SIZE(F_3) = 2 + 1 + 3 = 6$. Apparently program P_2 is

weaker than program P_1 because P_2 relies on files of bigger size, which is less likely to be assigned because of node capacity limits. The node environment weight measure is the sum of the link reliabilities surrounding that node for the node perfect case here, so $ENV_WEIGHT(N_1) = 0.9 + 0.8 = 1.7$, $ENV_WEIGHT(N_2) = 0.9 + 0.7 = 1.6$ and $ENV_WEIGHT(N_3) = 0.8 + 0.7 = 1.5$. The order of node environment weight measure is $N_1 > N_2 > N_3$.

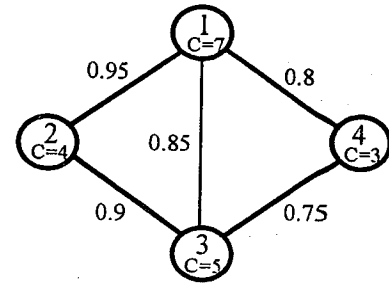
Next, we use MSR to choose good MFFCs. Based on the heuristic which put the weaker program to stronger nodes, we assign P_2 to N_1 , P_1 to N_2 and P_2 to N_3 . When the favorable order of assignments are determined, table 3 shows how the MFFC of each node is selected: Node N_1 is determined to be favored to Program P_2 , so we examine the table 3 to pick up the good MFFCs by the Minimum Selection Rule. Apparently $c_1 = \{P_2, F_1\}$ and $f_1 = \{F_3\}$ is our preferred choices. Continued this way we got $c_2 = \{P_1, F_1, F_2\}$ is the preferred MFFC for node N_2 and $e_3 = \{P_2, F_3\}$ is the choice for node N_3 . From table 3 we can see there are $6 \times 5 \times 7 = 210$ possible MFFC combinations for this case, and the Minimum Selection Rule effectively cut the choice from 210 to 2.

Table 3: The MSR applied to Example 3

| Node N_1 (MFFCs) | P_1 | P_2 |
|---------------------------|-----------------------|-----------------------|
| $a_1 = \{P_1, P_2\}$ | $F_1 + F_2 = 3$ | $F_1 + F_3 = 4$ |
| $b_1 = \{P_1, F_1\}$ | $F_2 = 2$ | $P_2 + F_3 = 5$ |
| $c_1 = \{P_2, F_1\}$ | $P_1 + F_2 = 3$ | $F_3 = 3$ |
| $d_1 = \{P_1, F_2\}$ | $F_1 = 1$ | $P_2 + F_1 + F_3 = 6$ |
| $e_1 = \{F_1, F_2\}$ | $P_1 = 1$ | $P_2 + F_3 = 5$ |
| $f_1 = \{F_3\}$ | $P_1 + F_1 + F_2 = 4$ | $P_2 + F_1 = 3$ |
| Node N_2 (MFFCs) | P_1 | P_2 |
| $a_2 = \{P_1, P_2, F_1\}$ | $F_2 = 2$ | $F_3 = 3$ |
| $b_2 = \{P_2, F_2\}$ | $P_1 + F_1 = 2$ | $F_1 + F_3 = 4$ |
| $c_2 = \{P_1, F_1, F_2\}$ | 0 | $P_2 + F_3 = 5$ |
| $d_2 = \{P_1, F_3\}$ | $F_1 + F_2 = 3$ | $P_2 + F_1 = 3$ |
| $e_2 = \{F_1, F_3\}$ | $P_1 + F_2 = 3$ | $P_2 = 2$ |
| Node N_3 (MFFCs) | P_1 | P_2 |
| $a_3 = \{P_1, P_2, F_1\}$ | $F_2 = 2$ | $F_3 = 3$ |
| $b_3 = \{P_1, P_2, F_2\}$ | $F_1 = 1$ | $F_1 + F_3 = 4$ |
| $c_3 = \{P_1, F_1, F_2\}$ | 0 | $P_2 + F_3 = 5$ |
| $d_3 = \{P_2, F_1, F_2\}$ | $P_1 = 1$ | $F_3 = 3$ |
| $e_3 = \{P_2, F_3\}$ | $P_1 + F_1 + F_2 = 4$ | $F_1 = 1$ |
| $f_3 = \{P_1, F_1, F_3\}$ | $F_2 = 2$ | $P_2 = 2$ |
| $g_3 = \{F_2, F_3\}$ | $P_1 + F_1 = 2$ | $P_2 + F_1 = 3$ |

Lastly, we apply the Grouping Rule to select our answer from two candidates. Both candidates have the full set $\{N_2, N_3\}$ so GR isn't useful in this case. However, it is irrelevant because both file assignments happened to deliver the optimal solution $R = 0.916$.

Example 4:



| Storage Capacity: | Program/File Size: | | Program Req.: |
|-------------------|--------------------|----------|----------------------|
| Node 1: 7 | $P_1: 1$ | $F_1: 1$ | $P_1: F_1, F_2, F_3$ |
| Node 2: 4 | $P_2: 2$ | $F_2: 2$ | $P_2: F_1, F_2, F_4$ |
| Node 3: 5 | $P_3: 3$ | $F_3: 3$ | $P_3: F_2, F_3, F_4$ |
| Node 4: 3 | | $F_4: 4$ | |

Figure 5. Network topology and data requirement of Example 4

The measure results of program weakness and node environment weight of Example 4 are listed below:
 $ENV_WEIGHT(N_1) = 2.6$ $WEAKNESS(P_1) = 7$
 $ENV_WEIGHT(N_2) = 1.85$ $WEAKNESS(P_2) = 9$
 $ENV_WEIGHT(N_3) = 2.5$ $WEAKNESS(P_3) = 12$
 $ENV_WEIGHT(N_4) = 1.55$

Follow the same heuristic, we put the weaker program to stronger nodes. When the favorable order of assignments are determined, we use the MSR to pick up the good MFFCs. Then we apply the Grouping Rule to select our answer from the candidates. Table 4 lists all the 5 possible heuristic guesses out of 24 in the Example 4. By applying our Grouping Rule, we know the second and the fifth ones (in bold face) are our preferred choices because they span only three nodes N_1, N_2 and N_3 . The last column of table 4 is the computed DSR values of each file assignment, which reflect the fact that our Grouping Rule is really quite effective. Table 5 shows the simulation results of Example 4.

Table 4: The file assignments and full set groups of Example 4

| | Node 1 | Node 2 | Node 3 | Node 4 | Full Set | DSR |
|---|----------------|---------------------|---------------------|-----------|----------------------|------------------|
| 1 | $\{F_3, F_4\}$ | $\{P_1, F_1, F_2\}$ | $\{P_2, F_1, F_2\}$ | $\{P_3\}$ | N_1, N_2, N_3, N_4 | 0.9549 |
| 2 | $\{P_3, F_4\}$ | $\{P_1, F_3\}$ | $\{P_2, F_1, F_2\}$ | $\{P_3\}$ | N_1, N_2, N_3 | 0.9787875 |
| 3 | $\{F_3, F_4\}$ | $\{P_1, F_3\}$ | $\{P_2, F_1, F_2\}$ | $\{P_3\}$ | N_1, N_2, N_3, N_4 | 0.9549 |
| 4 | $\{P_3, F_4\}$ | $\{P_1, F_1, F_2\}$ | $\{P_2, F_1, F_2\}$ | $\{F_3\}$ | N_1, N_2, N_3, N_4 | 0.9549 |
| 5 | $\{P_3, F_4\}$ | $\{P_1, F_3\}$ | $\{P_2, F_1, F_2\}$ | $\{F_3\}$ | N_1, N_2, N_3 | 0.9787875 |

Table 5: Simulation results of Example 4

| | | | |
|------------------------------|----------------------|-------------|--------|
| Number of MFFCs | 10,752 = (16x8x12x7) | | |
| Possible Heuristic Solutions | 24 | | |
| Heuristic Guesses | 5 | | |
| Speed Up Ratio | 448 = (10752/24) | | |
| DSR_{max} | 0.9787875 | DSR_{min} | 0.9549 |
| DSR_{SFA} | 0.9787875 | E_r | 0% |

where DSR_{max} = maximum DSR of random assignment
 DSR_{min} = minimum DSR of random assignment
 DSR_{SFA} = solution of SFA algorithm

$$E_r = \text{Relative error} = \frac{DSR_{max} - DSR_{SFA}}{DSR_{max} - DSR_{min}}$$

5. Summary and Conclusion

Distributed computing system has become a major trend in today's computer system design for its high fault-tolerance, potential for parallel processing and better reliability performance. One of the distributed computing system important characteristics is that it offers redundant copies of software to improve system's reliability. To effectively distribute these redundant copies of software to appropriate nodes is the basic consideration for file assignment problem. The problem has been proved to be an NP-problem. Traditional solution techniques such as back-tracking algorithm and mathematical programming can give the optimal solution, but they have to pay very high computation price as well as high storage problem. To effectively reduce problem space is an important research subject.

In this paper, we develop a heuristic algorithm called Simple File Assignment algorithm for the reliability-oriented file assignment problem to reduce the problem space. Based on the numerical simulation results, our simple file assignment algorithm obtain the exact solution in most cases with much improved computation time. Examples are given to illustrate the applicability of our approach. Simulation results are analyzed to justify the applicability and efficiency of our approach.

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